

SPECTRAL DENSITY FUNCTIONS FOR DIFFUSION THROUGH
DISORDERED MATERIALS

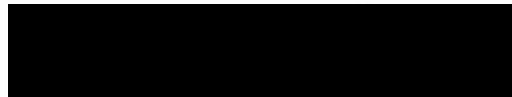
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A THESIS SUBMITTED AS A REQUIREMENT FOR THE DEGREE OF
MASTER OF SCIENCE OF
THE UNIVERSITY OF NEW ENGLAND
May 1996

DECLARATION

I certify that the substance of this thesis has not already been submitted for any degree and is not currently being submitted for any other degree.

I certify that to the best of my knowledge any help received in preparing this thesis, and all sources used, have been acknowledged in this thesis.



Acknowledgements

I would like to thank my supervisor, Associate Professor Colin Sholl for the help he has given me with my thesis. I would also like to thank my friends for keeping me going when things got tough. A special word of thanks and infinite appreciation for my parents who have made all of this possible.

For the LORD gives wisdom, and from his mouth comes knowledge and understanding. Proverbs 2:6.

Contents

| | |
|---|------------|
| Acknowledgements | iii |
| 1 Introduction | 1 |
| 1.1 Nuclear Spin Relaxation | 1 |
| 1.2 Hydrogen in Metals | 3 |
| 1.3 Types of Disorder | 4 |
| 2 Review | 7 |
| 2.1 Nuclear Spin Relaxation Rates | 7 |
| 2.2 Spin Jump Rates | 11 |
| 2.3 Ordered Systems | 12 |
| 2.4 Disordered Systems | 17 |
| 2.4.1 Structural Analysis | 17 |
| 2.4.2 Data Interpretation and Curve Fitting | 18 |
| 2.4.3 Monte Carlo Simulations | 21 |
| 3 Spectral Density Functions in Finite Systems | 26 |
| 3.1 Introduction | 26 |
| 3.2 The Rate Equation for Populations | 27 |
| 3.3 Comparison to Known Systems | 31 |
| 3.4 Eigenvalue and Coefficient Analysis | 37 |
| 3.5 Modifications for a Disordered System | 39 |
| 4 Application to Disordered Systems | 42 |
| 4.1 Introduction | 42 |
| 4.2 The Metallic Glass α -Zr ₃ RhH _{3.5} | 43 |

| | | |
|----------|--|-----------|
| 4.3 | Variation of Parameters in a Disordered System | 51 |
| 4.4 | Eigenvalues and Coefficients | 53 |
| 4.5 | Analytical Approximation | 56 |
| 5 | Conclusion | 61 |

List of Tables

| | |
|--|----|
| 3.1 Eigenvalues and Degeneracy for Ordered Diffusion on One Cube | 38 |
|--|----|

List of Figures

| | | |
|-----|---|----|
| 1.1 | Site Energy Disorder | 5 |
| 1.2 | Saddle Point Energy Disorder | 6 |
| 3.1 | Comparison between normalised spectral density functions for known models and computational method. | 36 |
| 3.2 | Histogram of eigenvalues and coefficients for a 12 cube, no disorder system. | 39 |
| 4.1 | Calculated relaxation rates R_1 (lower group of curves) and $R_{1\rho}$ (upper group) for site energy disorder (dashed curves) and saddle point energy disorder (solid curves). | 46 |
| 4.2 | Calculated relaxation rates R_1 (lower group of curves) and $R_{1\rho}$ (upper group) for site energy disorder with $P_{eq}(\mathbf{r}_i) = 1/N$ | 47 |
| 4.3 | Comparison between MCC fitted curve (dashed lines) and small, finite system model (solid lines). The lower group of curves are for R_1 , the upper for $R_{1\rho}$ | 48 |
| 4.4 | Calculated relaxation rates R_1 for four Gaussian widths | 49 |
| 4.5 | Position of peak heights (crosses) and positions (dots) as a function of the width of the Gaussian distribution. | 50 |
| 4.6 | Relaxation rates R_1 and $R_{1\rho}$ (arbitrary units) as a function of $\omega\tau$ for the simple cubic lattice and for two different resonant frequencies ω_0 (solid lines) and $2\omega_0$ (broken lines). | 51 |
| 4.7 | Relaxation rates for a Gaussian distribution of saddle point energies with $\sigma = 0.06$ and values of $\omega\tau_0 = 10^{-4}$ (solid curve), 10^{-5} (short dashed curve) and 10^{-6} (long dashed curve). | 53 |
| 4.8 | Histogram of eigenvalues and coefficients for a 4 cube disordered system, $\sigma = 0.03$ and $\sigma = 0.07$ | 54 |
| 4.9 | Comparison of histogram of eigenvalues and coefficients and fitted curve. | 57 |

| | |
|---|----|
| 4.10 Spectral density function for 12 cube system (solid line) and fitted curve (dashed lines). | 58 |
| 4.11 Comparison of exact (solid lines) and model function (dashed lines) for relaxation on a single cube. | 60 |