## REFERENCES

Adams, R. J. \& Khoo, S. 1993, Quest - The Interactive Test Analysis System, Melbourne: Australian Council for Educational Research.

Alexander, L. \& James, H. T. 1987, The Nation's Report Card, Cambridge, MA: National Academy of Education.

Andrews, G. 1996, Assessment of relational reasoning in children aged four to eight years, paper presented at the XIVth Biennial Meeting of the International Society for the Study of Behavioural Development, Quebec City, August 12-16, 1996.

Atweh, B. \& Watson, J. (Eds.) 1992, Research in Mathematical Education in Australasia 1988-1991, Brisbane: Mathematics Education Research Group of Australasia.

Battista, M. \& Clements, D. 1992, Students' cognitive construction of square and rectangles in logo geometry, in W. Geeslin \& K. Graham (Eds.), Proceedings of the Sixteenth Annual Conference of the International Group for the Psychology of Mathematics Education, (Vol. 1, pp. 57-64), Durham: Program Committee of the $16^{\text {th }}$ PME Conference.

Baturo, A. (Ed.) 1995, New Directions in Geometry Education, Brisbane: QUT Press.
Bennet, G. P. 1987, The Quality of Problem Solving in Mathematics, Masters of Education Thesis, Flinders University.

Biggs, J. B. \& Collis, K. F. 1982, Evaluating the Quality of Learning: The SOLO Taxonomy, New York: Academic Press.

Biggs, J. B. \& Collis, K. F. 1989, Towards a model of school-based curriculum development and assessment : Using the SOLO Taxonomy, Australian Journal of Education, 33 (2), 151-163.

Biggs, J. B. \& Collis, K. F. 1991, Multimodal learning and the quality of intelligent behaviour, in H. Rowe (Ed.), Intelligence: Reconceptualisation and Measurement, (pp. 57-76), Hillsdale, NJ: Lawrence Erlbaum Associates.

Board of Secondary Education, New South Wales 1988, Years 7-8 Mathematics Syllabus, North Sydney: Board of Secondary Education.

Board of Senior School Studies, New South Wales 1982, Years 11-12 Mathematics Syllabus, North Sydney: Board of Senior School Studies.

Board of Studies, New South Wales 1996a, Mathematics Years 9-10 Syllabus, Advanced Course Stage 5, North Sydney: Board of Studies.

Board of Studies, New South Wales 1996b, Mathematics Years 9-10 Syllabus, Intermediate Course Stage 5, North Sydney: Board of Studies.

Bordons, K. S. \& Abbott, B. B. 1991, Research Design and Methods: A Process Approach ( $2^{\text {nd }}$ Ed.), California: Mayfield.

Brainerd, C. J. 1973, Judgements and explanations as criteria for the presence of cognitive structures, Psychological Bulletin, 79, 172-179.

Brainerd, C. J. \& Kaszor, P. 1974, An analysis of supposed sources of children's class inclusion errors, Developmental Psychology, 10 (5), 633-643.

Bruner, J. S. 1964, The course of cognitive growth, American Psychologist, 19, 1-15.
Burger, W. F. 1985, Geometry. Arithmetic Teacher, 32 (6), 52-56.

Burger, W. F. \& Shaughnessy, J. M. 1986, Characterising the van Hiele Levels of development in Geometry, Journal for Research in Mathematics Education, 17 (1), 31-48.

Burgess, R. G. (Ed.) 1989, The Ethics of Educational Research, New York: The Falmer Press.

Burns, R. 1990, Introduction to research methods in education, Longman Cheshire: Melbourne.

Campbell, K. J., Watson, J. M. \& Collis, K. F. 1992, Volume measurement and intellectual development, Journal of Structural Learning, 11 (3) 279-298.

Campbell, R. L. 1991, Does class inclusion have mathematical prerequisites? Cognitive Development, 6, 169-194.

Carson, M. T. \& Abrahamson, A. 1976, Some members are more typical than others: The effect of semantic typicality on class inclusion performance, Child Development, 47, 1186-1190.

Case, R. 1985, Cognitive Development, New York: Academic Press.

Chapman, M. L. \& McBride, M. L. 1992, Beyond competence and performance: Children's class inclusion strategies, subordinate class cues, and verbal justifications, Developmental Psychology, 28, 319-327.

Chi, M. T. H. 1978, Knowledge structures and memory development, in R. Sieger (Ed.), Children's thinking: What develops? (pp. 73-96), Hillsdale, NJ: Erlbaum.

Clements, D. \& Battista, M. 1992, Geometry and spacial reasoning, in D. Grouws (Ed.), Handbook of Research on Mathematics Teaching and Learning (pp. 420-464), New York: Macmillan.

Coady, C. 1994, Investigations into tertiary students' understanding of variables, Doctoral Thesis, University of New England.

Coady, C. \& Pegg, J. E. 1993, A study of first year university students' interpretation of the meanings of letters used in algebraic contexts, Australian Senior Mathematics Journal, 7 (2), 21-31.

Cohen, L. \& Manion, L. 1994, Research Methods in Education (4 ${ }^{\text {th }}$ ed.), London: Routledge.

Collis, K. F. 1984, Development of a group test of mathematical understanding using super item/SOLO technique, Journal of Science and Mathematics Education in South East Asia, 1(1) 5-14.

Collis, K. F. 1992, Reshaping assessment practices: assessment in the mathematical sciences under challenge, in M. Stephens \& J. Izard (Eds.), Proceedings from the First National Conference on Assessment in the Mathematical Sciences (pp. 19-34), Geelong, Victoria: Australian Council of Educational Research.

Collis, K. F. \& Biggs, J. B. 1979, Classroom Examples of Cognitive Development Phenomena: The SOLO Taxonomy, Report prepared at conclusion of an Educational Research and Development Committee funded project.

Collis, K. F. \& Romberg, T. A. 1991, Assessment of mathematical performance: An analysis of open-ended test items, in M. C. Wittrock \& E. L. Baker (Eds.), Testing and Cognition, (pp. 82-130), Englewood Cliffs, NJ: Prentice-Hall.

Collis, K. F., Watson, J. \& Campbell, K. 1993, Cognitive functioning in mathematical problem-solving during early adolescence, Mathematics Education Research Journal, 5, 107-121.

Courtney, T. 1986, The significance of the SOLO Taxonomy for learning and teaching in Geography, Geographical Education, 5 (2), 47-50.

Coxford, A. F. 1978, Research directions in Geometry, in R. Lesh \& D. Mierkiewiscz (Eds.) Recent Research Concerning the Development of Spatial and Geometric Concepts (pp. 323-331), Columbus, Ohio: ERIC/SMEAC.

Crowley, M. L. 1987, The van Hiele model of the development of geometric thought, in M. Lindquist \& A. P. Shulte (Eds.), Learning and Teaching Geometry, K-12, (323-331), Virginia: NCTM.

Davey, G. \& Pegg, J. E. 1989, Relating of common 2-D shapes to underlying geometric concepts, paper presented at the twelfth annual conference of the Mathematics Research Group of Australasia, Bathurst, NSW.

Davey, G. \& Pegg, J. E. 1992, Research in Geometry and Measurement, in B. Atweh and J. Watson (Eds.), Research in Mathematical Education in Australasia 1988-1991, (pp. 231-247), Brisbane: Mathematics Education Research Group of Australasia.

Davidson, R. J., Schwartz, G. E. \& Shapiro, D. (Eds.) 1986, Consciousness and Self Regulation: Advances in Research, New York: Plenum Press.
de Villiers, M. D. 1987, Research evidence on hierarchical thinking strategies and the van Hiele Theory: some critical comments, Report No. 10 Research Unit for Mathematics Education, University of Stellenbosch.
de Villiers, M. D. 1993, The role and function of a hierarchical classification of quadrilaterals, Oral presentation at the Seventeeth Conference for the International Group for the Psychology of Mathematics Education, University of Tsukuba, Japan, $18^{\text {th }}-23^{\text {rd }}$ July 1993.

Diener, E. \& Crandall, R. 1978, Ethics in Social and Behavioural Research, Chicago: University of Chicago Press.

Drew, C. J., Hardman, M. L. \& Hart, A. W. 1996, Designing and Conducting Research: Inquiry in Education and Social Science, (2 $2^{\text {nd }}$ Ed), Needham Heights, Massachusetts: Allyn and Bacon.

Fischer, K. 1980, A theory of cognitive development: The control and construction of heirarchies of skills, Psychological Review, 57, 477-531.

Fischer, K. \& Pipp, S. 1984, Process of cognitive development: optimal level and skill acquisition, in R. Sternberg (Ed.), Mechanisms of Cognitive Development, (pp. 45-80), New York: W.H. Freeman.

Fischer, K. \& Silvern, L. 1985, Stages and individual differences in cognitive development, Annual Review of Psychology, 36, 613-648.

Fisher, W. (1993) Measurement-related problems in functional assessment, The American Journal of Occupational Therapy, 47, (4), 331-337.

Freudenthal, H. (Ed.). 1958, Report on Methods of Initiation into Geometry, Groningen: Wolters.

Freudenthal, H. 1973, Mathematics as an educational task. Dordrecht, Holland: Reidel.

Fuys, D. 1985, Van Hiele levels of thinking in Geometry, Education and Urban Society, 17, 447-462.

Fuys, D., Geddes, D. \& Tischler, R. (Eds.) 1984, English Translation of Selected Writings of Dina van Hiele-Geldof and Pierre M. van Hiele, New York: Brooklyn College.

Fuys, D., Geddes, D. \& Tischler, R. 1985, An Investigation of the van Hiele Model of Thinking in Geometry Among Adolescents, New York: Brooklyn College.

Fuys, D., Geddes, D. \& Tischler, R. 1988, The van Hiele Model of Thinking in Geometry among Adolescents, New York: Brooklyn College.

Goldstein, H. 1979, The Design and Analysis of Longitudinal Studies: Their role in the Measurement of Change, New York: Academic Press.

Greene, T. R. 1989, Children's understanding of class inclusion heirarchies: The relationship between representation and task performance, Journal of Experimental Child Psychology, 48 (1), 62-89.

Greene, T. R. 1991, Text manipulations influence children's understanding of class inclusion hierarchies, Journal of Experimental Child Psychology, (52), 354-374.

Greene, T. R. 1994, What kindergartens know about class inclusion hierarchies, Journal of Experimental Child Psychology, 57, 72-88.

Grouws, D. (Ed.). 1992, Handbook of Research on Mathematics Teaching and Learning, New York: Macmillan.

Gutierrez, A., Jaime, A. \& Fortuny, J. 1991, An alternative paradigm to evaluate the acquisition of the van Hiele levels, Journal for Research in Mathematics Education, 22 (3), 237-251.

Guiterrez, A., Jaime, A., Shaughnessy, J. M. \& Burger, W. 1991, A comparitive analysis of two ways of assessing the van Hiele levels of thinking, in F.Furinghetti (Ed.), Proceedings of the fifteenth annual conference of The International Group for the Psychology of Mathematics Education, (Vol. 2, pp. 109-116), Assissi: Program Committee.

Halford, G. S. 1982, The Development of Thought, Hillsdale, N. J.: Erlbaum.
Halford, G. S. 1996, Relational knowledge in higher cognitive processes, paper presented in symposium entitled Relational Knowledge in Higher Cognitive Processes at the XIVth Biennial Meeting of the International Society for the Study of Behavioural Development, Quebec City, August 12-16, 1996.

Hodkin, B. 1987, Performance analysis in class inclusion: An illustration with two language conditions, Developmental Psychology, 47, 32-38.

Hoffer, A. 1981, Geometry is more than proof, Mathematics Teacher, 74, 11-18.
Hoffer, A. 1983, Van Hiele-based research, in R. Lesh \& M. Landou (Eds.), Acquistion of Mathematics Concepts and Processes, (pp. 205-227), New York: Academic Press.

Hooper, F., Sipple, T., Goldman, J. \& Swinton, S. 1974, Technical Report No. 295, A cross-sectional investigation of children's classificatory abilities, University of Wisconsin Madison: Wisconsin Research and Development Centre for Cognitive Learning.

Hoyles, R. \& Noss, C. 1988, The computer as a mediating influence in the development of pupil's understanding of variable, European Journal of Psychology in Education, 3 (3), 271-286.

Inhelder, B. \& Piaget, J. 1964, The early growth of logic in the child: Classification and seriation, (E. A. Lunzer \& D. Papert, Trans, 1-16).

Jaime, A. \& Guiterrez, A. 1990, A Study of the degree of acquisition of the van Hiele levels in secondary school students, in Proceedings of the $14^{\text {th }}$ International Conference for the Psychology of Mathematics Education, (Vol. 2, pp. 251-258), Mexico: International Group for the Psychology of Mathematics Education.

Kerlinger, F. 1986, Foundations of Behavioural Research, Fortworth: Holt, Rinehart and Winston.

Kitwood, T. M. 1977, Values in adolescent life: towards a critical description, Ph.D thesis, School of Research in Education, University of Bradford.

Kofsky, E. 1963, Developmental scalogram analysis of classificatory behaviour, unpublished doctoral dissertation, University of Rochester.

Kofsky, E. 1966, A scalogram study of classificatory development, Child Development, 37, 191-204.

Lane, M. K. \& Hodkin, B. 1985, Role of atypical exemplars of social and nonsocial superordinate categories within the class inclusion paradigm, Developmental Psychology, 21, 909-915.

Lawrence, J. A. 1980, Class inclusion: Question order, Question Type, and Training, Senior Honors thesis, Memorial University of Newfoundland.

LeCompte, M. \& Goetz, J. P. 1982, Problems of reliability and validity in ethnographic research, Review of Educational Research, 52 (1), 31-60.

Lehrer, R. \& Chazan, C. (Eds.) 1998, New Directions For Teaching and Learning Geometry, New Jersey: L. Earlbum.

Lesh, R. \& Landou, M. (Eds.) 1983, Acquistion of Mathematics Concepts and Processes, New York: Academic Press.

Lesh, R. \& Mierkiewiscz, D. (Eds.) 1978, Recent Research Concerning the Development of Spatial and Geometric Concepts, Columbus, Ohio: ERIC/SMEAC.

Levins, L. 1992, Students' understanding of concepts related to evaporation, Research in Science Education, 22, 263-272.

Levins, L. \& Pegg, J. 1993, Students' understanding of concepts related to plant growth, Research in Science Education, 23, 165-173.

Lin, N. 1976, The Survey, Foundations of Social Research, New York: McGraw-Hill.
Lindquist, M. \& Shulte, A. P. (Eds.) 1987, Learning and Teaching Geometry, K-12, Virginia: NCTM.

Mammana, C. \& Kluwer, V. (Eds.) 1998, Perspectives on the Teaching of Geometry for the 21st Century, The Netherlands: Academic Publishers.

Markman, E. M. 1973, The facilitation of part-whole comparison by use of the collective noun "family", Child Development, 44, 837-840.

Markman, E. M. 1978, Empirical versus logical solutions to part-whole comparison problems concerning classes and collections, Child Development, 49, 168-177.

Markman, E. M. 1989, Categorisation and Naming in Children, Cambridge, MA: MT Press.

Martin, J. L. \& Bradbard, D. A. (Eds.) 1976, Space and geometry: papers from a research workshop, Athens, GA: University of Georgia, Georgia Centre for the Study of Learning and Teaching Mathematics.

Masters, G. N. 1982, A Rasch model for partial credit scoring, Psychometrica, 47 (2), 149-174.

Mayberry, J. 1981, An Investigation of the van Hiele Levels of Geometric Thought in Undergraduate Pre-Service Teachers, Thesis, Ed. D. University of Georgia.

Mayberry, J. 1983, The van Hiele levels of geometric thought in undergraduate preservice teachers, Journal for Research in Mathematics Education, 14 (1), 58-69.

Meltzoff, J. 1998, Critical Thinking about Research: Psychology and Related Fields, Washington DC: American Psychological Association.

Mulligan, J. \& Watson, J. 1998, A developmental mulitmodal model for multiplication and division, Mathematics Education Research Journal, 10 (2), 61-86.
$\mathrm{Ni}, \mathrm{Y} .1998$, Cognitive structure, content knowledge, and classificatory reasoning, Journal of Genetic Psychology, 159 (3), 280-297.

Norman, D. A. \& Shallice, T. 1986, Attention to action: Willed and automatic control of behaviour, in R. J. Davidson, G. E. Schwartz \& D. Shapiro (Eds.),

Consciousness and Self Regulation: Advances in Research (Vol 4, pp. 1-18), New York: Plenum Press.

Olive, J. 1991, Logo programming and geometric understanding: An in-depth study, Journal for Research in Mathematics Education, 22, 90-111.

Panizzon, D. 1999, Senior Secondary and early tertiary science students' developmental understandings of diffusion and osmosis: a Neo-piagetian approach, Ph.D Thesis, University of New England.

Pegg, J. E. 1992a, Students' understanding of Geometry: Theoretical perspectives, in B. Southwell, B. Perry \& K. Owens (Eds.), Space-The First and Final Frontier (pp. 18-36), Sydney: Mathematics Education Research Group of Australasia.

Pegg, J. E. 1992b, Assessing students' understanding at the primary and secondary levels in the mathematical sciences, in M. Stephens and J. Izard (Eds.), Reshaping Assessment Practices: Assessment in Mathematical Sciences Under Challenge, (pp. 368-385), Melbourne: Australian Council of Educational Research.

Pegg, J. E. 1996, Interpreting students' approaches to geometric proofs: A non-piagetian approach, in M. de Villiers \& F. Furinghetti (Eds.), Proofs and Proving: Why, When and How? $8^{\text {th }}$ International Conference on Mathematics Education, Topic Group on Proof, (pp. 101-108), Seville: ICME.

Pegg, J. E. 1997a, Mathematics Teaching-Creating the Future, in N.Scott \& H. Hollingsworth (Eds.), Mathematics Creating the Future, (pp. 20-38), Adelaide: Australian Association of Mathematics Teachers.

Pegg, J. E. 1997b, Broadening the descriptors of van Hieles' Levels 2 and 3, in F. Biddulp and K. Carr (Eds.), Proceedings of the 20th Mathematics Education Research Group of Australasia, (pp. 391-405), Rotorua, N.Z.: University of Waikato.

Pegg, J. E. \& Baker, P. 1999, An exploration of the interface between van Hiele's Levels 1 and 2: Initial findings, in O. Zaslavsky (Ed.), Proceedings of the $23^{\text {rd }}$ International Group for the Psychology of Mathematics Education, (Vol. 4, pp. 25-32), Haifa: Israel Institute of Technology.

Pegg, J. E. \& Currie, P. 1998, Widening the interpretation of van Hiele's Levels 2 and 3 in A. Oliver (Ed.), Proceedings of the 22nd International Group for the Psychology of Mathematics Education, (Vol. 2, pp. 216-223), Stellenbosch: University of Stellenbosch.

Pegg, J. E. \& Davey, G. 1989, Clarifying level descriptions for children's understanding of some basic 2D geometric shapes, Mathematics Education Research Journal, 1 (1), 16-27.

Pegg, J. E. \& Davey, G. 1991, Levels of geometric understanding, Australian Mathematics Teacher, 47 (2), 10-13.

Pegg, J. E. \& Davey, G. 1998, A synthesis of two models: Interpreting student understanding in Geometry, in R. Lehrer \& C. Chazan, (Eds.), New Directions For Teaching and Learning Geometry, (pp. 109-135), New Jersey: L. Earlbum.

Pegg, J. E. \& Faithful, M. 1995, Analysing higher order skills in deductive Geometry, in A. Baturo (Ed.), New Directions in Geometry Education, (pp. 100-105), Brisbane: QUT Press.

Pegg, J. E., Gutiérrez, A. \& Huerta, P. 1998, Assessing reasoning abilities in Geometry, in C. Mammana \& V. Villani, Kluwer (Eds.), Perspectives on the Teaching of Geometry for the 21st Century, (pp. 275-295), The Netherlands: Academic Publishers.

Pegg, J. E. \& Woolley, S. 1994, An investigation of strategies used to solve a simple deductive exercise in Geometry, in G. Bell, B. Wright, N. Leeson \& J. Geake (Eds.), Challenges in Mathematics education: Constraints of construction, Proceedings of the fourteenth annual conference of the Mathematics Research Group of Australasia (pp. 472-479), Lismore, New South Wales: Mathematics Education Research Group of Australasia. .

Piaget, J. 1965, The Child's Concept of Number, New York: Norton. (original work published 1941).

Piaget, J. 1970, Science of Education and Psychology of the Child, New York: Basic Books.

Piel, J. A. 1987, Developmental pacing as an alternative to ability grouping in a primary setting, Eric Document: ED285640, Ohio, U.S.

Rabinowitz, F. M., Howe, M. L. \& Lawrence, J. A. 1989, Class inclusion and working memory, Journal of Experimental Child Psychology, 48 (3), 379-409.

Reading, C. \& Pegg, J. 1996, Exploring understanding of data reduction, in Gutierrez, A. (Ed.), Proceedings of the 20th International Group for the Psychology of

Mathematics Education, (Vol. 4, pp. 187-195), Valencia, Spain: International Group for the Psychology of Mathematics Education.

Reese, H. W. \& Shack, M. L. 1974, Comment on Brainard's criteria for cognitive structures, Psychological Bulletin, 81, 67-69.

Romberg, T. A. 1992, Perspectives on scholarship and research methods, in D. Grouws (Ed.), Handbook of Research on Mathematics Teaching and Learning, (pp. 49-64), New York: Macmillan.

Rowe, H. (Ed.) 1991, Intelligence: Reconceptualisation and Measurement, (pp. 57-76), Hillsdale, NJ: Lawrence Erlbaum Associates.

Sarantakos, S. 1998, Social Research, South Melbourne: Macmillan Education.

Scott, N. \& Hollingsworth, H. (Eds.), Mathematics Creating the Future, Adelaide: Australian Association of Mathematics Teachers.

Senk, S. 1989, Van Hiele levels and achievement in writing geometry proofs, Journal for Research in Mathematics Education, 20 (3), 309-332.

Siegel, L. S. 1978, The relationships of language and thought in the preoperational child: A reconsideration of nonverbal alternatives to Piagetian tasks, in L.S. Siegel \& C.J. Brainerd (Eds.), Alternatives to Piaget, (pp. 43-67), San Diego, CA: Academic Press.

Siegel, L.S. \& Brainerd, C.J. (Eds.) 1978, Alternatives to Piaget, San Diego, CA: Academic Press.

Southwell, B., Perry, B. \& Owens, K. (Eds.) 1992, Space-The First and Final Frontier, Sydney: Mathematics Education Research Group of Australasia.

Stanbridge, B. 1990, Making science more accessable to students: A curriculum based on cognitive criteria, Australian Science Teachers' Journal, 36 (2), 7-14.

Stephens, M. \& Izard, J. (Eds.) 1992, Reshaping Assessment Practices: Assessment in Mathematical Sciences Under Challenge, Melbourne: Australian Council of Educational Research.

Sternberg, R. (Ed.) 1984, Mechanisms of Cognitive Development, New York: W.H. Freeman.

Thomas, H. \& Horton, J. J. 1997, Competency criteria and the class inclusion task: Modeling judgements and justifications, Developmental Psychology, 33 (6), 1060-1073.

University of New England (accessed 31 Aug. 1999) UNE Research Services, Research Ethics, http://rs-nt-10. une.edu.au/Home/V_2_1/ethics.htm.

Usiskin, Z. 1982, Van Hiele levels and achievement in secondary school geometry (Final report of the Cognitive Development and Achievement in Secondary School Geometry Project), Chicago, IL: University of Chicago, Department of Education.

Usiskin, Z. \& Senk, S. L. 1990, Evaluating a test of van Hiele levels: a response to Crowley and Wilson, Journal for Research in Mathematics Education, 21, 242-245.
van Hiele, P. M. 1955, De niveau's in het denkin, welke van belang zijn bij het onderwijs in de meetkunde in de eerste klasse van het V.H.M.O. In Pedagogische Studien, XXXII (pp. 289-297), Groningen: Wolters, in van Hiele, P.M., 1986, Structure and Insight: a theory of Mathematics education, New York: Academic Press.
van Hiele, P.M. 1959, Development and Learning Process: A study of some aspects of Piaget's psychology in relation with the didactics of Mathematics, Institute of Education, University of Utrecht, No. XV11, Groningen: Wolters.
van Hiele, P. M. 1986, Structure and insight: a theory of Mathematics education, New York: Academic Press.
van Hiele, P. M., \& van Hiele-Geldof, D. 1958, A method of initiation into Geometry, in H. Freudenthal (Ed.), Report on Methods of Initiation into Geometry, Groningen: Wolters.

Watson, J., Campbell, K. J. \& Collis, K. 1992, Ikonic and early concrete symbolic responses to two fraction problems, in W. Gleeson \& K. Graham (Ed.), Proceedings of the Sixteenth International Group for the Psychology of Mathematics Education Conference, 3, (pp. 139). Durham: International Group for Psychology of Mathematics Education.

Watson, J. M., Collis, K. F., Callingham, R. A. \& Moritz, J. B. 1995, A model for assessing higher order thinking in statistics, Educational Research and Evaluation, 1 (3), 247-275.

Watson, J. M., Collis, K. F. \& Moritz, J. B. 1997, The development of chance measurement, Mathematics Education Research Journal, 9 (1), 60-82.

Watson, J. \& Mulligan, J. 1990, Mapping solutions to an early multiplication word problem, Mathematics Education Research Journal, 2 (2), 28-44.

White, P. \& Mitchelmore, M. 1997, Recognition of abstract angles in familiar physical situations, in F. Biddulph \& K. Carr, People in Mathematics Education, Proceedings of the $20^{\text {sh }}$ Annual Conference of the Mathematics Education Research Group of Australasia, (pp. 577-584), Waikato: Mathematics Education Research Group of Australasia.

Whitland, J. \& Pegg, J. E. 1999, Exploring Diversity: Year 2 students' responses to questions concerning simple 2D shapes, in J.M. Truran \& K.M. Truran (Eds.), Making the Difference, Proceedings of the 22nd Annual Conference of The Mathematics Education Research Group of Australasia, (pp. 546-553), University of Adelaide: Mathematics Education Research Group of Australasia.

Wiersma, W. 1991, Research Methods in Education: An Introduction, Boston: Allyn and Bacon.

Wilson, M. 1990, Measuring a Van Hiele Geometry Sequence: A Reanalysis, Journal For Research in Mathematics Education, 21 (3), 230-237.

Wirzup, I. 1976, Breakthroughs in the psychology of learning and teaching geometry, in J.L. Martin \& D.A. Bradbard (Eds.), Space and geometry: papers from a research workshop, (pp. 75-97), Athens, GA: University of Georgia, Georgia Centre for the Study of Learning and Teaching Mathematics.

Wittrock, M. C. \& Baker, E. L. (Eds.) 1991, Testing and Cognition, Englewood Cliffs, NJ: Prentice-Hall.

## APPENDIX A

## PILOT STUDY

## Section 1: Relationships among figures

Part A: Relationships among triangles
Int: These cards have been placed into two groups. Can you tell me the way in which the cards have been sorted? (initial question to focus the student within the context of triangles and quadrilaterals)


Int: I would like you to sort them into smaller groups. As you sort them I would like you to explain your reasons for sorting them the way you have chosen.
Probes include: Why have you placed these triangles together?
Why is this triangle on its own?
Is there anything else that you can tell me about the groups?
Prompts include: Are there any other ways that the triangles can be sorted?
What reasons do you think someone might have for placing the equilateral in with the isosceles? What would you think about doing that?

## Part B: $\quad$ Relationships among quadrilaterals

The format above was repeated with the 6 quadrilateral cards below.


## Section 2: Relationships among properties

## Part A: Relationships among triangle properties

Int: I would like you to think about all that you know about the equilateral triangle. Tell me all the properties that belong to that figure (these were listed on cards by the interviewer).

Int: I want you to think very carefully now, as I would like you to come up with a description or definition that accurately refers to that shape with the least number of properties needed.
Int: Come up with as many combinations as you can.
Probes include: Why would your friend need that combination of cards? Why is it possible to remove these cards?
Prompts include: What would happen if I removed this card? Would your friend still recognise the triangle? Why?

Questions repeated for the right isosceles triangle.

Part B: Relationships among quadrilateral properties
Format above repeated for the square, rhombus, and parallelogram.

## APPENDIX B

## STUDIES 1 AND 2 INTERVIEW PROFORMA

## Study 1: Triangles

## Phase 1: Relationships among triangle figures

(i) Int: I would like you to write a list of all the triangle names you can think of. Begin with acute-angled scalene. Draw each triangle.
(ii) Int: Design a tree diagram which links the different triangles. Draw a sketch to link each type.
(discussion follows concerning the reasons for links and/or lack of links) (the following three points are addressed if required)
(iii) Int: There are some triangles that we can add to this list. (provide triangles not recalled)
Draw a sketch of each new triangle.
(iv) Int: Design a second tree diagram incorporating all the triangles on the list. (discussion follows concerning the reasons for links and/or lack of links)
(v) Int: Return now to your first map. I would like you to add the new triangles to your original tree. (discussion follows concerning the reasons for links and/or lack of links)

## Study 2: Quadrilaterals

## Phase 1: Relationships among quadrilateral figures

(i) Int: I would like you to write a list of all the quadrilateral names you can think of. Draw each quadrilateral.
(ii) Int: Design a tree diagram which links the different quadrilaterals. Draw a sketch to link each type. (discussion follows concerning the reasons for links and/or lack of links) (the following three points are addressed if required)
(iii) Int: There are some quadrilaterals that we can add to this list. (provide quadrilaterals not recalled)
Draw a sketch of each new quadrilateral.
(iv) Int: Design a second tree diagram incorporating all the quadrilateralson the list. (discussion follows concerning the reasons for links and lack of links)
(v) Int: Return now to your first map. I would like you to add the new quadrilaterals to your original tree. (discussion follows concerning the reasons for links and/or lack of links)

## Study 1: Triangles

## Phase 2: Relationships among triangle properties

(i) Int: We are going to look closely at a few triangles.

I have placed some cards in front of you with triangle characteristics on them.
I would like you to begin by choosing the cards which belong to the equilateral triangle (selection made).
Look carefully to make sure that you have included all the cards, which belong to that triangle.
(ii) Int: Suppose you wanted to leave some clues for a friend.

Do you think that your friend would need to see all these properties to know that you are thinking about an equilateral triangle?
What combination could you leave? (discussion follows concerning reasons for cards included in the combination and those that have been removed)
Do you think it could be made simpler? (discussion follows concerning reason for the simplification and inability to make simpler)
(iii) Int: Let's put all the cards back. I would like you to make a different set of clues for your friend. (point (ii) repeated until student has provided all known combinations).
(iv) First three steps repeated for the right isosceles triangle.

Triangle Characteristic Cards
3 SIDES
3ANGLES
3 SIDES EQUAL
3ANGLES EQUAL
HAS RIGHT ANGLE
1AXIS OF SYMMETRY
NOAXES OF SYMMETRY
3AXES OF SYMMETRY
HAS OBTUSEANGLB
HAS ACUTEANGLES
2ANGLES EQUAL
2 SIDES EQUAL

## Study 1: Quadrilaterals

## Phase 2: Relationships among quadrilateral properties

(i) Int: We are going to look closely at a few quadrilaterals.

I have placed some cards in front of you with quadrilateral characteristics on them (see below).
I would like you to begin by choosing the cards which belong to the square (selection made).

Look carefully to make sure that you have included all the cards, which belong to the square.
(ii) Int: Suppose you wanted to leave some clues for a friend.

Do you think that your friend would need to see all these properties to know that you are thinking about a square?
What combination could you leave? (discussion follows concerning reasons for cards included in the combination and those that have been removed)
Do you think it could be made simpler? (discussion follows concerning reason for the simplificationand inability to make simpler)
(iii) Int: Lets put all the cards back. I would like you to make a different set of clues for your friend. (point (ii) repeated until student has provided all known combinations).
(iv) First three steps repeated for parallelogramand rhombus.

Quadrilateral Characteristic Cards
4SIDES
4ANGLES
ALL SIDES ARE EQUAL
THEREARE 4 RIGHT ANGLES
OPPOSITE SIDES ARE PARALLEL
OPPOSITE SIDES ARE EQUAL
DAGONALS AREEQUAL
DIAGONALS BISECT
DAGONALS MEET AT RIGHT ANGLES OPPOSITEANGLES ARE EQUAL
2PAIR OF EQUALADJACENT SIDES
1 PAIR OF OPPOSITEANGLES EQUAL
4AXES OF SYMMETRY
2AXES OF SYMMETRY
1AXIS OF SYMMETRY
1 PAIR OF PARALLEL SIDES
1PAIR OF OPPOSITE SIDES EQUAL

## APPENDIX C

## INTERVIEW RESOURCES

Student Profile

Name:

School: $\qquad$

Year:

Age:

## Study 1 Part 1: List of triangle names and sketches

Triangle tree diagram - 1 and 3

Triangle tree diagram 2

## Study 2 Part 1: List of quadrilateral names and sketches

Quadrilateral tree diagram - 1 and 3

Quadrilateral tree diagram 2

Study 1 Part 2: Triangle property characteristic cards

| 3 SIDES |
| :---: |
| T1 |
| 3 ANGLES |
| T2 |
| 3 SIDES EQUAL |
| T3 |
| 3 ANGLES EQUAL |
| T4 |
| HAS RIGHT ANGLE |
| T5 |
| 1 AXIS OF SYMMETRY |
| T6 |
| NO AXES OF SYMMETRY |
| T7 |
| 3 AXES OF SYMMETRY |
| T8 |
| HAS OBTUSE ANGLE |
| T9 |
| HAS ACUTE ANGLES |
| T10 |
| 2 ANGLES EQUAL |
| T11 |
| 2 SIDES EQUAL |
| T12 |

## Students triangle property choice

## 1. Equilateral triangle



## 2. Right isosceles triangle



Study 1 Part 2: Quadrilateral property characteristic cards

| $\begin{gathered} 4 \text { SIDES } \\ \text { Q1 } \\ \hline \end{gathered}$ |
| :---: |
| $\begin{gathered} 4 \text { ANGLES } \\ \mathrm{Q} 2 \\ \hline \end{gathered}$ |
| ALL SIDES ARE EQUAL Q3 |
| THERE ARE 4 RIGHT ANGLES $\mathrm{Q} 4$ |
| OPPOSITE SIDES ARE PARALLEL Q5 |
| OPPOSITE SIDES ARE EQUAL Q6 |
| DIAGONALS ARE EQUAL Q7 |
| DIAGONALS BISECT Q8 |
| DIAGONALS MEET AT RIGHT ANGLES Q9 |
| OPPOSITE ANGLES ARE EQUAL Q10 |
| 2 PAIR OF EQUAL ADJACENT SIDES Q11 |
| 1 PAIR OF OPPOSITE ANGLES EQUAL Q12 |
| 4 AXES OF SYMMETRY Q13 |


| 2 AXES OF SYMMETRY |
| :---: |
| Q14 |
| 1 AXIS OF SYMMETRY |
| Q15 |
| 1 PAIR OF PARALLEL SIDES |
| Q16 |
| 1 PAIR OF OPPOSITE SIDES EQUAL |
| Q17 |

## Students Quadrilateral Property Choice

1. Square

First Choice
$\begin{array}{llllllllllll}1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12\end{array}$ $\begin{array}{lllll}13 & 14 & 15 & 16 & 17\end{array}$
Minimum Information
$\begin{array}{llllllllllll}1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12\end{array}$ $\begin{array}{lllll}13 & 14 & 15 & 16 & 17\end{array}$
Made Simpler
$\begin{array}{llllllllllll}1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12\end{array}$ $\begin{array}{lllll}13 & 14 & 15 & 16 & 17\end{array}$
Other Combination
$\begin{array}{llllllllllll}1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12\end{array}$ $\begin{array}{lllll}13 & 14 & 15 & 16 & 17\end{array}$
Other Combination
$\begin{array}{llllllllllll}1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12\end{array}$ $\begin{array}{lllll}13 & 14 & 15 & 16 & 17\end{array}$
Other Combination
$\begin{array}{llllllllllll}1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12\end{array}$ $\begin{array}{lllll}13 & 14 & 15 & 16 & 17\end{array}$

## 2. Parallelogram

First Choice
$\begin{array}{llllllllllll}1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12\end{array}$
$\begin{array}{lllll}13 & 14 & 15 & 16 & 17\end{array}$
Minimum Information
$\begin{array}{llllllllllll}1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12\end{array}$ $\begin{array}{lllll}13 & 14 & 15 & 16 & 17\end{array}$
Made Simpler
$\begin{array}{llllllllllll}1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12\end{array}$ $\begin{array}{lllll}13 & 14 & 15 & 16 & 17\end{array}$
Other Combination
$\begin{array}{llllllllllll}1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12\end{array}$
$\begin{array}{lllll}13 & 14 & 15 & 16 & 17\end{array}$
Other Combination
$\begin{array}{llllllllllll}1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12\end{array}$
$\begin{array}{lllll}13 & 14 & 15 & 16 & 17\end{array}$
Other Combination
$\begin{array}{llllllllllll}1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12\end{array}$ $\begin{array}{lllll}13 & 14 & 15 & 16 & 17\end{array}$

| 3. Rhombus |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| First Choice |  |  |  |  |  |  |  |  |  |  |  |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| 13 | 14 | 15 | 16 | 17 |  |  |  |  |  |  |  |
| Minimum Information |  |  |  |  |  |  |  |  |  |  |  |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| 13 | 14 | 15 | 16 | 17 |  |  |  |  |  |  |  |
| Made Simpler |  |  |  |  |  |  |  |  |  |  |  |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| 13 | 14 | 15 | 16 | 17 |  |  |  |  |  |  |  |
| Other Combination |  |  |  |  |  |  |  |  |  |  |  |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| 13 | 14 | 15 | 16 | 17 |  |  |  |  |  |  |  |
| Other Combination |  |  |  |  |  |  |  |  |  |  |  |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| 13 | 14 | 15 | 16 | 17 |  |  |  |  |  |  |  |
| Other Combination |  |  |  |  |  |  |  |  |  |  |  |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| 13 | 14 | 15 | 16 | 17 |  |  |  |  |  |  |  |

## APPENDIX D

## INTRARATER AND INTERRATER RELIABILITY

To enable a measurement of the congruity of the system utilised to code students' responses to tasks concerning relationships among figures, and relationships among quadrilaterals, it was necessary to calculate both intrarater and interrater reliability. In an attempt to measure intrarater reliability the consistency the researcher's coding between responses is assessed. Interrater reliability requires a co-marker to utilise the described marking scheme and compare this coding against the principal researcher's coding. This assessment is discussed below.

Firstly, intrarater reliability was established through the random selection of one quarter of the students' responses to each of the seven tasks across Years 8-12. The percentage of responses, which were categorised into the same SOLO levels in both the initial codings and subsequent codings, was $96 \%$.

Secondly, another researcher who has considerable experience working within the SOLO model over many years then coded the randomly selected sample of one quarter of the responses. For each of the seven tasks, the researcher worked within the described structure of levels for each particular task. The measure of agreement between the principal researcher and the co-marker was $92 \%$.

Throughout the coding process, the consistency of the SOLO Model was also established via consultation between researcher and co-marker when rare difficulties occurred with categorisation of particular responses. This was particularly necessary in transitional cases. Overall, the following measures ascertained coding reliability for the SOLO model.

## APPENDIX E

## PLAIN LANGUAGE STATEMENT / CONSENT FORM

Dear Parent / Guardian,
I am currently completing a Ph.D at the University of New England. As part of this program I am undertaking a study to investigate students' growth and understanding in Geometry. The focus of the study is to be on Years 8 to 12 students in Armidale High Schools. The purpose of this letter is to request your permission to include your son/daughter/ward as a participant in the study.

The study, which has the support of the Principal of the school, is designed in such a way that disruption to the normal school process will be minimal. It will consist of each student being interviewed on one occasion for approximately 40 minutes. At a later date each student will also be required to complete some pen and paper tasks. The interviews will be audiotaped for later analysis but there will be complete confidentiality for both students and schools with the use of pseudonyms where necessary. All records will be held within the Centre of Cognitive Research in Learning and Teaching (CRiLT).

The title of the project is "An investigation of students' understanding of class inclusion concepts in Geometry." Associate Professor John Pegg from the Department of Curriculum Studies, UNE, will also be involved in the study.

Participation by your son/daughter/ward is entirely voluntary and he/she will not be penalised for not wishing to be involved. It is also possible for the participant to withdraw consent and discontinue participation at any time.

If you have any concerns or enquiries you can contact me (Ph 73 5073), Assoc. Prof. John Pegg (Ph 73 5070) or the Principal for further information. If you are willing to allow your son/daughter/ward to participate could you please complete the attached consent form and return it to the school.

If your son / daugter / ward is selected at random as a participant, a letter will be sent to you before the commencement of interviews.

Should you have any complaints concerning the manner in which this research is conducted, please contact the Ethics Committee at the following address:

The Secretary
Human Research Ethics Committee
Research Services
University of New England
Armidale, NSW 2351
Telephone: (067) 732352 Facsimile (067) 733543

Yours Faithfully,

Penelope Serow
Ph.D Student

## Student Consent

I, $\qquad$ (the participant) have read the information concerning the study and any questions I have asked have been answered to my satisfaction. I agree to participate in this activity, realising that I may withdraw at any time. I agree that research data gathered for this study may be published, provided my name is not used.

Student Signature

Date

## Parent /Guardian Consent

I, $\qquad$ (parent/guardian) have read the information concerning the study and any questions I have asked have been answered to my satisfaction. I give permission for my son/daughter/ward to be a participant in this study, realising that my child may withdraw at any time. I agree that research data gathered for this study may be published, provided my child's name is not used.

Parent / Guardian Signature

Date

## APPENDIX F

## RELATIONSHIPS AMONG TRIANGLES TASK ANALYSIS

A student's response concerning the relationships among triangles could include one of three sets of triangle relationships and the reasons for these links. The three sets of relationships, which could be identified and justified, are based on similar features, independent triangle-type classes, and triangle-type classes involving class inclusion.

## Set 1: Relationships based on similar features

There are three types of features upon which students could link triangles, namely, angle types (Figure F.1), side lengths and angle sizes (Figure F.2), and symmetry (Figure F.3).
a) Angle Types

In Figure F. 1 triangles are linked on one of three angle types. A student would select a feature and then link triangles that are seen to contain that feature.


Figure F. 1 Angle-type triangle classes
b) Sides and/or Angles

In Figure F. 2 the triangles are linked based on the properties associated with equality of sides and/or angles. The alternatives are three sides/angles equal, two sides/angles equal, and no sides/angles equal.

Three sides and/or three angles equal.


Two sides and/or two angles equal.


No sides and/or no angles equal.


Figure F. 2 Relationships based on equality sides and/or angles
c) Symmetry

In Figure 4.3 the existence of symmetry is the defining feature. Here there are three possibilities, which are three axes of symmetry, one axis of symmetry, and no axes of symmetry.

Three axes of symmetry


One axis of symmetry


> No axis of symmetry


Figure F. 3 Relationships based on symmetry

Set 2: The establishment of three triangle-type classes, namely, scalene, isosceles, and equilateral (Figure F.4).


Figure F. 4 Triangle type classes

In Figure F. 4 the triangles are linked based on properties, such as equality of sides/angles, and/or the number of axes of symmetry. These combine to establish an identified and independent class of triangles.

Set 3: The relationships among the triangle types incorporate the notion of class inclusion (Figure F.5).


Figure F. 5 Class inclusion incorporating triangle-type relationships

The equilateral triangle is a subset of the isosceles class of triangles. This relationship exists because the equilateral triangle is seen to include in its list of properties, the properties of an isosceles triangle, i.e., two sides/two angles equal and one axis of symmetry.

Overall, the task analysis provides a number of expected outcomes that might be considered plausible possibilities. Of interest is whether students provide these possibilities, whether there is some sequencing of the responses in terms of development, and the nature of the thinking that accompanies the responses.

## APPENDIX G

## RELATIONSHIPS AMONG QUADRILATERALS TASK ANALYSIS

It is necessary to consider all possible elements of a response addressing the relationships between the six quadrilaterals focused upon in the interview, prior to coding into groups. A response concerning the relationships among quadrilaterals include two sets of relationships and the reasons for these links. These being:

## Set 1: Relationships based on similar properties

In Figures G.1, G.2, G.3, G.4, and G.5, the quadrilaterals are linked based on the properties associated with equality of sides, equality of angles, symmetry, diagonals, and parallelism.
a) Sides


All sides equal.


Opposite sides equal


Adjacent sides equal.
Figure G. 1 Relationships based on side properties.
b) Angles


Figure G. 2 Relationships based on angle properties
c) Symmetry


Four axes of symmetry.


At least two axes of symmetry


At least one axis of symmetry.


Figure G. 3 Relationships based on symmetry properties
d) Diagonals


Figure G. 4 Relationships based on diagonal properties
e) Parallelism


Opposite sides parallel.


Figure G. 5 Relationships based on parallelism.

Set 2: The establishment of three quadrilateral classes involving subsets with justification for each class based on properties such as sides, angles, symmetry, and diagonals (Figure 5.6).

The three classes include;
a) Rectangle
b) Rhombus
c) Parallelogram


Figure G. 6 Quadrilateral classes involving subsets

## APPENDIX H

QUADRILATERAL PROPERTIES TASKS CONTEXTUAL GROUPINGS

| Student | Square | Parallelogram | Rhombus |
| :---: | :---: | :---: | :---: |
| Scott | 3 | 3 | 2 |
| Jason | 2 | 2 | 3 |
| Brendan | 1 | 2 | 2 |
| Kathy | 2 | 3 | 3 |
| Louise | 3 | 2 | 3 |
| Narelle | 2 | 3 | 3 |
| Peter | 2 | 3 | 2 |
| Andrew | 2 | 2 | 3 |
| Arthur | 3 | 2 | 3 |
| Alice | 2 | 2 | 3 |
| Megan | 3 | 2 | 2 |
| Ellen | 2 | 3 | 2 |
| Nathan | 1 | 2 | 2 |
| Adam | 2 | 2 | 2 |
| Allan | 1 | 2 | 2 |
| Frances | 2 | 2 | 2 |
| Suzanne | 1 | 2 | 1 |
| Tracy | 2 | 2 | 2 |
| Cameron | 2 | 3 | 3 |
| Michael | 2 | 2 | 3 |
| David | 1 | 2 | 2 |
| Beth | 1 | 3 | 2 |
| Dianne | 2 | 3 | 2 |
| Jenny | 2 | 3 | 3 |

## APPENDIX I

SOLO RESPONSE CODINGS FOR STUDIES 1, 2, AND 3

|  | ID | 1. Tri | 2. Quad | 3. Equ | 4. Isos | 5. Squ | 6. Para | 7. Rhom |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Scott | 101 | M2/R2 (CS) | M2 (CS) | U1 (F) | U1 (F) | U1 (F) | R2 (CS) | U2 (CS) |
| Jason | 102 | R2 cat 1 (CS) | M2 (CS) | U1 (F) | U1 (F) | M1 (F) | R1 (F) | M2 (CS) |
| Brendan | 103 | M2 (CS) | U2 (F) | R2 (CS) | M2 (CS) | R2 (CS) | M1 (F) | M1 (F) |
| Kathy | 104 | R2 cat 2 (CS) | M2 (CS) | M2 (CS) | R2 (CS) | U2 (CS) | M1 (F) | M2 (CS) |
| Louise | 105 | M2/R2 (CS) | M2 (CS) | R2 (CS) | R2 (CS) | U1 (F) | U1 (F) | M1 (F) |
| Narelle | 106 | R1 (CS) | R1 (CS) | M2 (CS) | M2 (CS) | R2 (CS) | R2 (CS) | U2 (CS) |
| Peter | 107 | U2 cat 1 (CS) | M2 (CS) | U1 (F) | U2 (CS) | U1 (F) | R2 (CS) | U1 (F) |
| Andrew | 108 | M2 (CS) | M2 (CS) | M2 (CS) | U1 (F) | R2 (CS) | M1 (F) | M2 (CS) |
| Arthur | 109 | U2 cat 1(CS) | M2 (CS) | M2 (CS) | U1 (F) | R2 (CS) | U1 (F) | M2 (CS) |
| Alice | 110 | M2 (CS) | M2/R2 (CS) | R1 (CS) | M2 (CS) | U1 (F) | M2 (CS) | M1 (F) |
| Megan | 111 | M2 (CS) | U2 (CS) | M1 (F) | U1 (F) | R2 (CS) | R2 (CS) | U1 (F) |
| Ellen | 112 | U 2 cat 2 (CS) | M2 (CS) | R1 (CS) | U2 (CS) | M2 (CS) | R2 (CS) | U1 (F) |
| Nathan | 113 | U1 (F) | R1 (F) | M2 (CS) | M2 (CS) | M1 (F) | R1 (F) | U2 (F) |
| Adam | 114 | U2 (F) | R1 (F) | U1 (F) | R2 (CS) | M1 (F) | M1 (F) | M1 (F) |
| Allan | 115 | R2 cat 2 (CS) | R2 (CS) | M1 (F) | U1/M1 (F) | M1 (F) | M1 (F) | R2 (CS) |
| Frances | 116 | R2 cat 3 (CS) | R1 (CS) | M2 (CS) | U2 (F) | U1 (F) | M2 (CS) | M2 (CS) |
| Suzanne | 117 | M2/R2 (CS) | M2/R2 (CS) | M2 (CS) | M2 (CS) | U1 (F) | M2 (CS) | U1 (F) |
| Tracy | 118 | U2 cat 2 (CS) | R1 (CS) | U1 (F) | U1 (F) | M1 (F) | U1 (F) | R2 (CS) |
| Cameron | 119 | R2 cat 1 (CS) | U2 (CS) | U1 (F) | U1 (F) | M1 (F) | M1 (F) | U1 (F) |
| Michael | 120 | R2 cat 2 (CS) | R2 (CS) | U1 (F) | M2 (CS) | M1 (F) | R2 (CS) | U1 (F) |
| David | 121 | R1 (F) | R1 (F) | U1 (F) | U1 (F) | U2 (CS) | U2 (F) | R2 (CS) |
| Beth | 122 | R2 cat 4 (CS) | M2/R2 (CS) | U1 (F) | R2 (CS) | U1 (F) | R1 (F) | U2 (F) |
| Dianne | 123 | M1 (F) | R2 (CS) | M2 (CS) | R2 (CS) | R2 (CS) | U1 (F) | R2 (CS) |
| Jenny | 124 | R2 cat 1 (CS) | R2 (CS) | R1 (CS) | U1/M1 (F) | M2 (CS) | U1 (F) | U1 (F) |
| Scott | 201 | R2 (CS) | R2 (CS) | U2 (F) | M1 (F) | R1 (F) | U2 (F) | U1 (F) |
| Jason | 202 | U2 (F) | $\mathrm{U} 2(\mathrm{~F})$ | U2 (F) | U2 (F) | M1 (F) | U2 (F) | U2 (F) |
| Brendan | 203 | M2 (CS) | U2 (F) | U2 (F) | U1 (F) | U2 (F) | U2 (F) | M1 (F) |
| Kathy | 204 | M2/R2 (CS) | M2/R2 (CS) | U1/M1 (F) | U2 (F) | U1 (F) | U1 (F) | U1 (F) |
| Louise | 205 | M2/R2 (CS) | R2 (CS) | M1 (F) | M1 (F) | M1 (F) | M1 (F) | U1 (F) |
| Narelle | 206 | R1 (F) | R2 (CS) | M1 (F) | U2 (F) | M1 (F) | U1 (F) | M1 (F) |
| Peter | 207 | R2 (CS) | M2 (CS) | U1/M1 (F) | M2 (CS) | M1 (F) | U1 (F) | M1 (F) |
| Andrew | 208 | M2 (CS) | R2 (CS) | R1 (F) | U1 (F) | M1 (F) | M1 (F) | M1 (F) |
| Arthur | 209 | R2 (CS) | M2/R2 (CS) | U1 (F) | U1 (F) | M1 (F) | R1 (CS) | M1 (F) |
| Alice | 210 | M2 (CS) | M2 (CS) | U2 (F) | U2 (F) | M1 (F) | M1 (F) | R2 (CS) |
| Megan | 211 | R2 (CS) | R2 (CS) | M2 (CS) | U1 (F) | R2 (CS) | M2 (CS) | U1 (F) |
| Ellen | 212 | M2 (CS) | R2 (CS) | U1/M1 (F) | U2 (CS) | R2 (CS) | U2 (CS) | R2 (CS) |

## APPENDIX J

RASCH ANALYSIS CODING

|  | ID | 1. <br> Tri | 2. <br> Quad | 3. <br> Equ | $\mathbf{4 .}$ <br> Isos | $\mathbf{5 .}$ <br> Squ | $\mathbf{6 .}$ <br> Para | Rhom <br> Rhom |
| :---: | :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Scott | 101 | 3 | 3 | 5 | 5 | 5 | 4 | 2 |
| Jason | 102 | 4 | 3 | 5 | 5 | 6 | 7 | 3 |
| Brendan | 103 | 3 | 8 | 4 | 3 | 4 | 6 | 6 |
| Kathy | 104 | 4 | 3 | 3 | 4 | 2 | 6 | 3 |
| Louise | 105 | 3 | 3 | 4 | 4 | 5 | 5 | 6 |
| Narelle | 106 | 1 | 1 | 3 | 3 | 4 | 4 | 2 |
| Peter | 107 | 2 | 3 | 5 | 2 | 5 | 4 | 5 |
| Andrew | 108 | 3 | 3 | 3 | 5 | 4 | 6 | 3 |
| Arthur | 109 | 2 | 3 | 3 | 5 | 4 | 5 | 3 |
| Alice | 110 | 3 | 3 | 1 | 3 | 5 | 3 | 6 |
| Megan | 111 | 3 | 2 | 6 | 5 | 4 | 4 | 5 |
| Ellen | 112 | 2 | 3 | 1 | 2 | 3 | 4 | 5 |
| Nathan | 113 | 5 | 7 | 3 | 3 | 6 | 7 | 8 |
| Adam | 114 | 8 | 7 | 5 | 4 | 6 | 6 | 6 |
| Allan | 115 | 4 | 4 | 6 | 5 | 6 | 6 | 4 |
| Frances | 116 | 4 | 1 | 3 | 8 | 5 | 3 | 3 |
| Suzanne | 117 | 3 | 3 | 3 | 3 | 5 | 3 | 5 |
| Tracy | 118 | 2 | 1 | 5 | 5 | 6 | 5 | 4 |
| Cameron | 119 | 4 | 2 | 5 | 5 | 6 | 6 | 5 |
| Michael | 120 | 4 | 4 | 5 | 3 | 6 | 4 | 5 |
| David | 121 | 7 | 7 | 5 | 5 | 2 | 8 | 4 |
| Beth | 122 | 4 | 3 | 5 | 4 | 5 | 7 | 8 |
| Dianne | 123 | 6 | 4 | 3 | 4 | 4 | 5 | 4 |
| Jenny | 124 | 4 | 4 | 1 | 5 | 3 | 5 | 5 |
| Scott | 201 | 4 | 4 | 8 | 6 | 7 | 8 | 5 |
| Jason | 202 | 8 | 8 | 8 | 8 | 6 | 8 | 8 |
| Brendan | 203 | 3 | 8 | 8 | 5 | 8 | 8 | 6 |
| Kathy | 204 | 3 | 3 | 5 | 8 | 5 | 5 | 5 |
| Louise | 205 | 3 | 4 | 6 | 6 | 6 | 6 | 5 |
| Narelle | 206 | 7 | 4 | 6 | 8 | 6 | 5 | 6 |
| Peter | 207 | 4 | 3 | 5 | 3 | 6 | 5 | 6 |
| Andrew | 208 | 3 | 4 | 7 | 5 | 6 | 6 | 6 |
| Arthur | 209 | 4 | 3 | 5 | 5 | 6 | 1 | 6 |
| Alice | 210 | 3 | 3 | 8 | 8 | 6 | 6 | 4 |
| Megan | 211 | 4 | 4 | 3 | 5 | 4 | 3 | 5 |
| Ellen | 212 | 3 | 4 | 5 | 2 | 4 | 2 | 4 |
|  |  |  |  |  |  |  |  |  |

Key: $\quad \mathbf{1}=\mathrm{R}_{1}(\mathrm{CS}), \quad 2=\mathrm{U}_{2}(\mathrm{CS}), \quad \mathbf{3}=\mathrm{M}_{2}(\mathrm{CS}), \quad 4=\mathbf{R}_{2}(\mathrm{CS})$,
$\mathbf{5}=\mathrm{U}_{1}(\mathrm{~F}), \quad \mathbf{6}=\mathrm{M}_{1}(\mathrm{~F}), \quad \mathbf{7}=\mathrm{R}_{1}(\mathrm{~F}), \quad \mathbf{8}=\mathrm{U}_{2}(\mathrm{~F})$

