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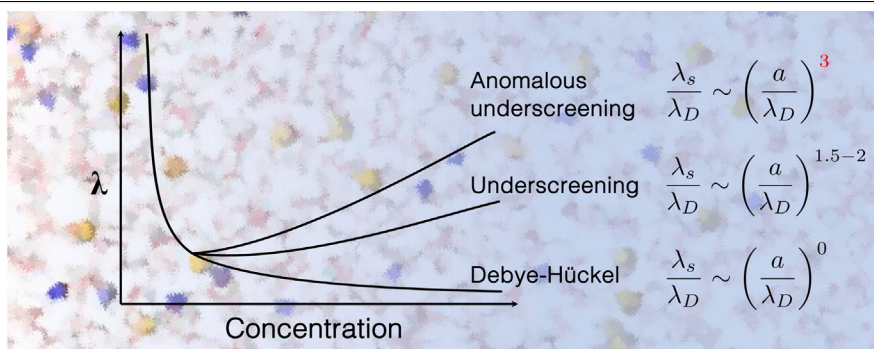
The known-unknowns of anomalous underscreening in concentrated electrolytes

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HIGHLIGHTS

- Anomalous underscreening is the experimentally-observed phenomenon in which the electrostatic decay length increases with ionic strengths in a manner that cannot be explained via electrolyte theories or simulations.
- We present a comprehensive review of recent theoretical and experimental work aiming to understand anomalous underscreening in concentrated electrolytes.
- We highlight numerous factors that, while potentially important to understanding this phenomenon, have not yet been examined by those working in this field of research.

GRAPHICAL ABSTRACT



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ABSTRACT

Electrolytes are central to life and technology but lack complete understanding. Recent experiments with highly concentrated electrolytes have revealed electrostatic decay lengths orders of magnitude larger than those predicted by theory and simulation. This phenomenon, dubbed 'anomalous underscreening' and its origin is still lack a comprehensive understanding. Herein we provide a perspective over recent developments in this field and discuss phenomena that, while potentially pertinent to electrolyte underscreening, are yet to be fully explored - i.e. the 'known-unknowns' of electrostatic underscreening in concentrated electrolytes.

1. Introduction

Electrolytes are of fundamental importance to a vast array of chemical, biological and physical phenomena. They are central to power

storage and green energy technologies (e.g. batteries [1–3] and supercapacitors [4–6]), global geophysical phenomena (e.g. weather [7] and oceans [8–10]) and underpin modern agriculture (e.g. *via* fertilisers and

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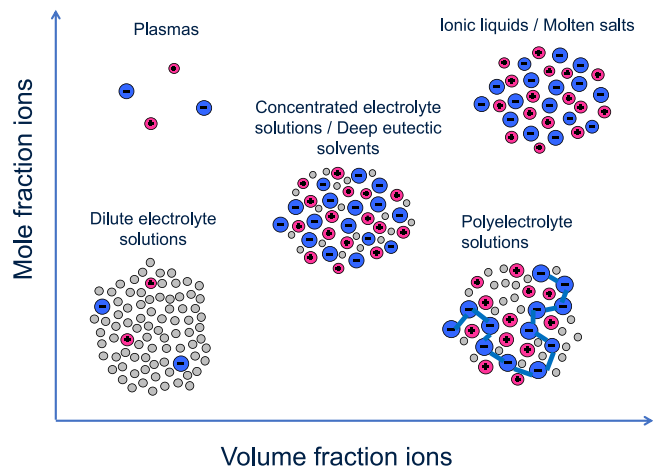


Fig. 1. The spectrum of electrolytes, comprising systems that include or consist entirely of charged species that interact with each other via Coulomb interactions. The density of the charges influences how strong these interactions are, and can be visualised as volume fraction (i.e. density of all species) and mole fraction (number of the species that are ions). Plasmas, while not being an electrolyte, are included for comparison since theoretical treatments of electrolytes share some commonalities [41].

nutrients) [11]. Indeed, life as we know it would not exist without electrolytes [12–15].

Electrolytes comprise charged atomic or molecular species that are dominated by long-range Coulomb interactions. They can exist with other species present (i.e. solvents) and at various concentrations, and this leads to a range of systems that include dilute electrolytes, concentrated (“hypersaline” or “salt-in-solvent”) electrolytes [16–19], polymer-based electrolytes [20–26], polyelectrolytes [27–30], deep eutectic solvents (DES) [31,32], ionic liquids (ILs) [33] and molten salts [34] (Fig. 1). Each of the systems shown in Fig. 1 are themselves active areas of research. However, they are unified in the sense that they manifest “ion-specific” physicochemical phenomena [35–39], whereby behaviour and properties are determined by the identity of the ions present, not just their charge or concentration. For such systems the addition of ions do not merely perturb their properties, it drives fundamental changes to them, even at low electrolyte concentration [40].

The presence of ions in solvents generates substantial electric fields [42]. Intermolecular interactions within electrolytes are therefore predominantly Coulombic. While the Coulombic potential from a lone charge in vacuum (or dielectric medium) decays as $1/r$ (where r is the radial distance from the charge), in an electrolyte the potential decays more rapidly due to the presence of other ionic and molecular species and their collective interactions and motions. Indeed, ions in solvents also alter solvent-solvent interactions [43–51], including long-range orientational correlations [52–55]. These local electric fields drive the diffusion of mobile charges to achieve local charge neutrality, a phenomenon known as screening [56]. The most commonly employed model of this phenomenon is the well-known Debye–Hückel [57] (DH) theory (discussed further in Section 2), which predicts in dilute electrolytes a shorter-ranged decay of the form $e^{\alpha r}/r$ [58,59]. The constant α here modulates the length scale of the decay and is a proxy for the extent of the Coulombic screening provided by the surrounding dielectric medium. The length scale associated with this screening is $\lambda_D = 1/\alpha$, which is the distance over which the potential decays to $1/e$ of its initial value [60] - this distance is commonly known as the screening length, or Debye length.

The screening length is a critical property of any electrolyte and is known to influence the conformation and stability of colloidal particles [61–64], lipid phases [65], enzymes [66] and DNA [67,68]. Even fundamental properties of electrolytes, such as conductivity [69–73]

and double layer structure [74–76], are influenced by the decay length of the local electrostatic potential. A recent review has also discussed the link between the double layer structure and electrocatalytic activity [77]. Beyond dilute concentrations however, deviations from the prediction of DH theory are observed. This is clearly seen in Fig. 2, which shows measured screening lengths as a function of concentration contradict the predictions of DH theory (dashed line). This deviation is known as underscreening (i.e. the mean electrostatic potential is screened less than predicted by DH theory, i.e. it is “under” screened). However, the magnitude of this phenomenon varies between theory and experiment (and between experiments themselves). This has led to underscreening being classified as either *normal* or *anomalous* [78] (see Fig. 2).

To date, no satisfactory explanation that unifies observations of anomalous underscreening with theoretical predictions has been proposed. In this perspective, we therefore summarise recent theoretical and experimental investigations of underscreening in electrolytes. We begin by detailing the key classical theories describing electrostatic interactions in electrolytes (Section 2) and the theoretical origins of underscreening (Section 3). Experiments demonstrating anomalous underscreening are discussed in Section 4. We conclude the perspective by presenting results that highlight the importance of (so-far overlooked) factors related to underscreening, to highlight potential avenues of future research into this intriguing phenomenon (Section 5).

2. Conventional electrolyte models: Poisson–Boltzmann and Debye–Hückel theories

The conventional models of electrolytes are derived from the Poisson equation, which relates the electrostatic potential (ψ) to the charge density (ρ) in a dielectric medium [58,106]:

$$-\epsilon_0 \epsilon_r \nabla^2 \psi(r) = \rho(r) \quad (1)$$

Here the relative permittivity of the medium is ϵ_r , ϵ_0 is the vacuum permittivity and ∇^2 is the Laplacian operator. A solution to Eq. (1) can be obtained by considering a reference ion and computing Coulombic interactions with other point-charge ions in the system to give the charge density $\rho(r)$. Assuming Boltzmann statistics gives the Poisson–Boltzmann (PB) equation itself:

$$-\epsilon_0 \epsilon_r \nabla^2 \psi(r) = q n^b e^{-q\psi(r)/k_B T} \quad (2)$$

where q is the reference ion charge, n^b is the ensemble number density, k_B is the Boltzmann constant, and T is the temperature. General solutions to the PB equation must be calculated numerically. However, in the case where the potential is small, the exponential can be linearised and the solution written in closed form [58]. This linearisation of Eq. (2) is otherwise known as the Debye–Hückel equation [57,58]:

$$\nabla^2 \psi_i(r) = \begin{cases} 0, & 0 < r < a \\ \kappa_D^2 \psi_i(r), & r \geq a \end{cases} \quad (3)$$

where a is the diameter of the reference ion. The eigenvalue κ_D^2 of this equation is given by:

$$\kappa_D^2 = \frac{1}{k_B T \epsilon_r \epsilon_0} \sum_j q_j^2 n_j^b \quad (4)$$

with the Debye length (electrostatic decay length) related by $\lambda_D = \kappa_D^{-1}$. For an electrolyte with known concentration, Eq. (4) can be re-written (using $\lambda_D = \kappa_D^{-1}$) as:

$$\lambda_D = \sqrt{\frac{k_B T \epsilon_r \epsilon_0}{2 q_e^2 N_A I}} = \frac{1}{\sqrt{8 \pi \lambda_B N_A I}} \quad (5)$$

where $I = \sum_j z_j^2 c_j^b / 2$ is the ionic strength, $c_j^b = n_j^b / N_A$ is the bulk concentration of species j (in mol/m³) with formal charge z_j , and q_e is the electron charge. The equality on the right hand side is an alternate definition of λ_D which uses the Bjerrum length, λ_B , which is

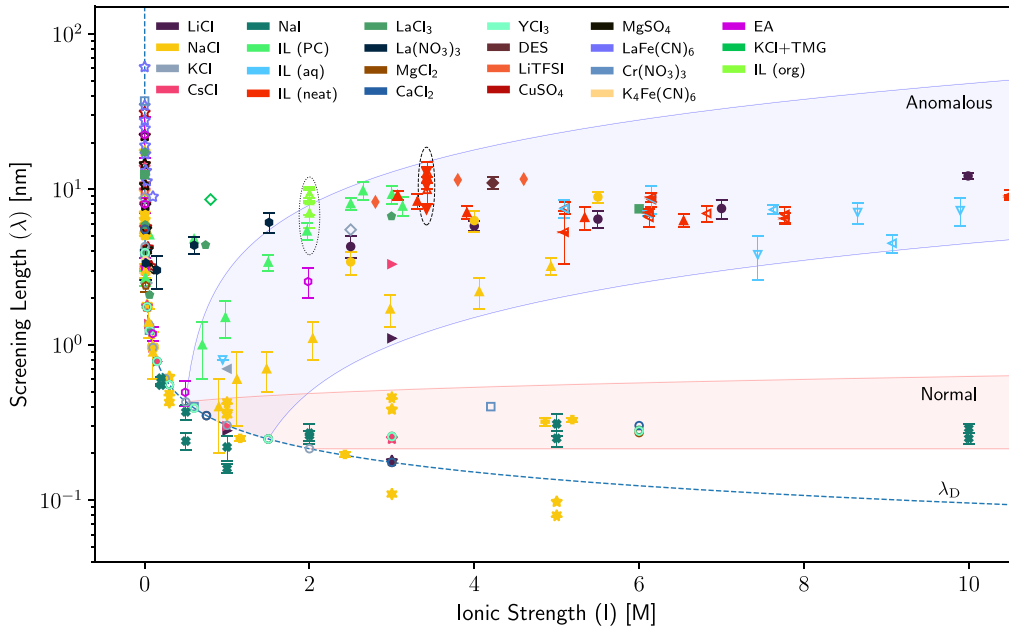


Fig. 2. Concentrated electrolytes exhibit underscreening, whereby the observed screening length λ_s becomes larger than that predicted by Debye-Hückel theory (λ_D). A collation of experimental and theoretical results indicates underscreening and anomalous underscreening in various concentrated electrolytes. Data series are coloured according to salt/solution, while symbols indicate the source of the data and the experimental/theoretical technique used. Data corresponds to aqueous solutions at 298 K unless otherwise specified. Triangles or polygons refer to surface force balance (SFB) experiments for various electrolytes: $\blacktriangle$ Ref. [79], $\blacktriangleleft$ Ref. [80], $\blacktriangleright$ Ref. [81], $\blacktriangledown$ Ref. [82], $\triangle$ Ref. [83], ∇ Ref. [84], $\triangleleft$ Ref. [85], $\triangleleft$ Ref. [86], $\triangleleft$ Ref. [87], $\triangle$ Refs. [88,89], $\blacktriangle$ Ref. [90], $\blacksquare$ Ref. [91], $\bullet$ Ref. [92], $\circ$ Ref. [93], $\diamond$ Ref. [94], $\diamond$ (with 0.5 M TMG) Ref. [95], $\blacklozenge$ Ref. [96], $\square$ Ref. [91], $\circ$ Ref. [97], $\circ$ Ref. [98]. Stars refer to atomic force microscopy (AFM): $\star$ Ref. [99], $\star$ (pH fixed equal to 9) Ref. [99], $\star$ (temperature set to 318 K) Ref. [99], $\star$ Ref. [100]. Filled circles ($\bullet$) refer to fluorescence measurements from Ref. [101], open circles ($\circ$) refer to λ^* from Ref. [102]. All-atom molecular dynamics (MD) simulations are given by $\times$ Ref. [103] and $+$ Ref. [104]. The dashed ellipse highlights SFB measurements on $[\text{C}_4\text{C}_1\text{im}][\text{NTf}_2]$ (∇ , $\triangle$) where the applied potential was varied [82,83], showing the resulting variation in the value of λ_s within the anomalous regime. The dotted ellipse highlights the variation of λ_s determined from 2 M solutions of $[\text{C}_4\text{C}_1\text{pyrr}][\text{NTf}_2]$ ($\blacktriangle$, $\triangle$) in several organic solvents [79,89]. Several chemicals are abbreviated as follows: propylene carbonate (PC), trimethylglycine (TMG), ethanolamine (EA). The density of $[\text{C}_4\text{C}_1\text{im}][\text{NTf}_2]$ was calculated using data from Ref. [105].

the distance at which the *unscreened* electrostatic interaction energy is equivalent to the thermal energy $k_B T$:

$$\lambda_B = \frac{q_e^2}{4\pi k_B T \epsilon_r \epsilon_0} \quad (6)$$

Both Eqs. (2) and (5) predict that screened electrostatic potential around the reference ion decreases monotonically, as determined by the unique decay length λ_D . This decay length itself is predicted to decrease with increasing ionic strength. To gauge the effect of the linearisation of Eq. (2) (i.e. using the DH instead of the PB theory), activity coefficients γ obtained using both theories are compared in Fig. 3(a) [107]. This figure gauges the influence of linearisation of the PB equation via the ratio $\gamma_{PB}/\gamma_{LPPB}$; any deviation from $\gamma_{PB}/\gamma_{LPPB} = 1$ indicates that DH-theory incurs spurious errors in γ . Fig. 3(a) shows that, generally, DH-theory performs reasonably for monovalent (1:1) salts for a wide concentration range. However, it is immediate from this figure that for any non-1:1 electrolyte the DH assumption is not justified, although some of the n:1 or 1:n salts do gain better agreement with the PB theory at higher concentrations. What is not obvious from Fig. 3 is that the PB equation itself becomes increasingly unreliable at higher concentrations due to the assumptions that (a) the distribution of ions surrounding the reference charge is not correlated and that (b) the ions themselves lack finite size effects. Further, atomic force microscopy (AFM) measurements of Smith et al. [100], Fig. 3(b), show deviations from DH theory (as indicated by the ratio $\kappa/\kappa_D \neq 1$) for multivalent ions at much lower concentrations. One of the major reasons for these deviations is that the PB and DH theories treat electrostatics as strictly local; i.e. the potential at a given point is determined only by that point, and not by the surrounding neighbourhood [58,108]. In addition, the absence of finite-size ions in the theory is also detrimental to its predictive utility.

Additionally, the PB/DH theories are used in mean-field descriptions of the electrical double layer (EDL), specifically to describe the charge decay in the diffuse layer. Briefly, the typical mean-field model is known as the Gouy-Chapman-Stern model, which has been built up from various theories beginning with the simple capacitor model of Helmholtz [109,110]. It is now thought to contain a proximal region known as the Stern layer [111], which is split (due to Grahame [112]) into the inner Helmholtz plane (IHP), where adsorbed ions have lost part of their solvation shell, and the outer Helmholtz plane (OHP), where the solvation shells are still intact. This is then followed by the diffuse layer, which is the entry point for the PB/DH theory, as introduced by Gouy [113] and Chapman [114]. The thickness of this layer is colloquially described as coinciding with the bulk screening length (λ), although multiple Debye lengths are actually needed for the decay to reach zero. This model is widely used, and assumed to be comprehensive, despite the shortcomings [77,115–117] due to surface coupling (see Section 5.2) and the limitations of the PB/DH theories.

Concentrated (and multivalent) electrolytes therefore necessitate the use of more sophisticated electrolyte theories. This is also true of the dynamic counterpart, the Debye-Hückel-Onsager (DHO) theory [118–120], which is concerned with predicting electrolyte conductivity. For example, the inclusion of finite-sized ions has recently been shown to give reasonable agreement with experiment [70,71]. Similarly, various other models based on PB and DH theory aim to improve their predictions to higher concentrations either by adding additional terms describing different physical effects, such as finite size effects [121, 122], or by including empirical parameters which may or may not describe physical properties, such as in specific ion interaction theory (SIT) [123,124] and the Pitzer equations [125,126]. Further discussion on the derivations and limits of DH theory has recently been reported by Kontogeorgis and co-workers [107,127,128].

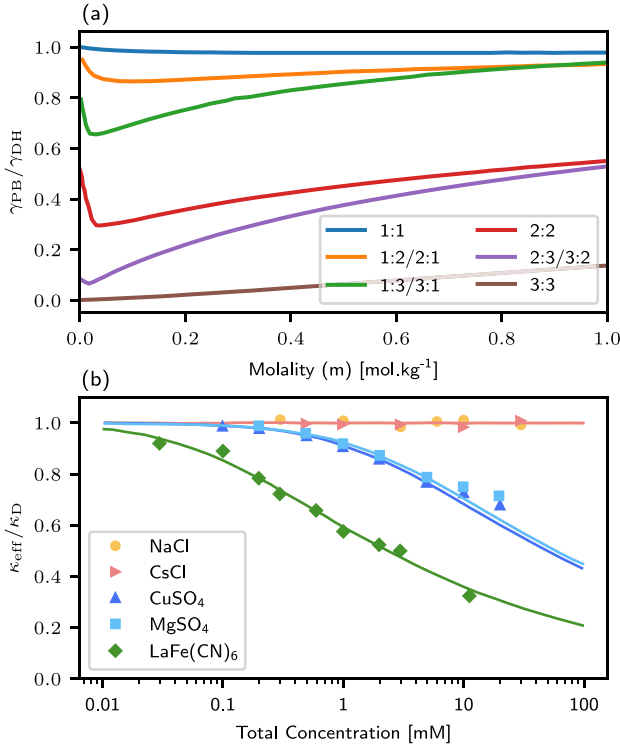


Fig. 3. The shortcomings of conventional electrolyte models. (a) Activity coefficients: γ_{PB} and γ_{DH} give the PB-predicted and DH-predicted coefficients, respectively. Reproduced with permission from Silva et al. [107]. (b) Experimental AFM measurements by Smith et al. [100], showing the significant deviations from DH theory at low concentrations for multivalent electrolytes. Note the different x-scale. Source: Data reproduced from Refs. [100,107].

3. Beyond Debye–Hückel theory - Origins of underscreening

3.1. The influence of finite ion size

The monotonic electrostatic decay length predicted by the PB and DH equations is the result of considering the reference ion differently to the ions in the surrounding ion cloud (which are treated as uncorrelated point charges). In 1936, Kirkwood presented a theoretical derivation that treated all ions with finite size, and predicted a crossover at high concentrations from the Yukawa-like decay behaviour, to a damped exponential form. This transition point (from monotonic decay to oscillatory decay) bears Kirkwood's name, and arises solely from the finite ion size included in the model. This approach was revisited in a later work by Kirkwood and Poirier [121], and more recently by Kjellander and co-workers, who employed the dressed ion/molecule theory (DIT/DMT) [129–134], which treats all ions consistently as finite sized particles and incorporates nonlocal electrostatics. This statistical mechanical treatment gives the following equation for κ :

$$\kappa^2 = \frac{1}{\lambda} = \frac{1}{k_B T \mathcal{E}_r^*(k) \epsilon_0} \sum_j n_j^b q_j q_j^* \quad (7)$$

where q_j^* is the “dressed” charge of ion species j that accounts for nonlocal electrostatics by taking into account the charges in the neighbourhood of the particle [135]. $\mathcal{E}_r^*(k)$ is given by:

$$\mathcal{E}_r^*(\kappa) = 1 + \frac{1}{\epsilon_0} \int r^2 \left[\frac{\sinh(\kappa r) - \kappa r}{(\kappa r)^3} \right] \chi^*(r) dr \quad (8)$$

and provides a more sophisticated description of the permittivity (compared to the simple relative permittivity ϵ_r) that is dependent on κ and the polarisation response function $\chi^*(r)$ [136]. Under this framework,

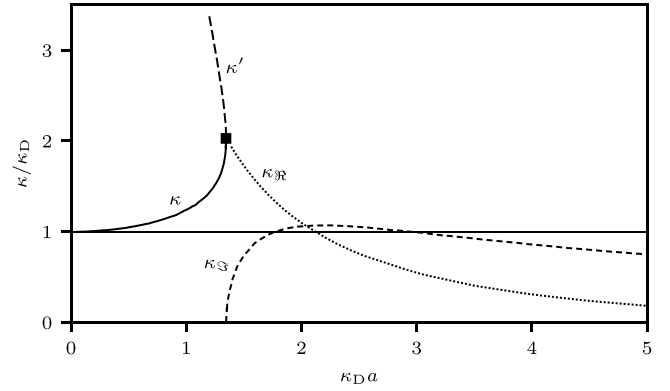


Fig. 4. Solutions to Eq. (9) for a 1:1 electrolyte at room temperature. Deviations from the horizontal line at κ/κ_D indicate deviations from DH theory (i.e. where $\kappa = \kappa_D$). At low concentrations (i.e. low $\kappa_D a$), the dominant solution is κ , however as $\kappa_D a$ increases, κ' will be increasingly non-negligible. At the Kirkwood point (indicated by ■), $\kappa = \kappa'$ and then at higher concentrations the solution becomes complex, with $\kappa = \kappa_R \pm i\kappa_I$, indicating the onset of the damped oscillatory behaviour. In this theory, the onset of normal underscreening occurs at $\kappa_{DH} a \approx 2$, where $\kappa/\kappa_D < 1$. Redrawn after Kjellander [138].

strongly correlated ions (e.g. ion pairs) will not contribute to q_j^* , but will contribute (as dipoles) to the value of $\mathcal{E}_r^*(k)$ [108].

While these revised theories are analytically exact, if some constraints are imposed (e.g. so that it resembles a DH-like form [137,138], with finite sized particles with dressed/effective charges), the deviation between DH-predicted κ_D and the simplified DIT theory (κ) can be calculated via [138]:

$$\left[\frac{\kappa}{\kappa_D} \right]^2 = \frac{e^a}{1 + \kappa a} \quad (9)$$

Eq. (9) gives two solutions, and these are shown in Fig. 4 for a 1:1 electrolyte at room temperature. At low $\kappa_D a$ ($\propto \sqrt{I}$) the electrostatic potential exhibits typical Yukawa decay [139]:

$$\psi_i(r) \sim C_i \frac{e^{-\kappa r}}{r} + C_i' \frac{e^{-\kappa' r}}{r} \quad (10)$$

where C_i and C_i' are constants associated with the two decay lengths $\lambda = 1/\kappa$ and $\lambda' = 1/\kappa'$. Of these, κ dominates as κ' is large and decays quickly. As $\kappa_D a \rightarrow 0$, $\kappa \rightarrow \kappa_D$ i.e. at very low concentrations DH behaviour is recovered (indicated by $\kappa/\kappa_D = 1$). Interestingly, at non-zero $\kappa_D a$, the decay length of the primary response (κ) is predicted to decay faster than DH theory ($\kappa/\kappa_D > 1$). The theory predicts that κ and κ' will converge at the Kirkwood point (≈ 1.2 for the example 1:1 electrolyte considered in Fig. 4), at which point the solutions $\kappa = \kappa_R \pm i\kappa_I$ become complex conjugates (with real and imaginary parts κ_R and κ_I , respectively). In this regime the electrostatic potential exhibits oscillatory decay (first shown by Kirkwood [140]) such that [139]:

$$\psi_i(r) \sim B_i \cos(\kappa_I r + \vartheta_i^c) \frac{e^{-\kappa_R r}}{r} \quad (11)$$

where $1/\kappa_R$ is the decay length, $2\pi/\kappa_I$ is the wavelength of the oscillation (associated with the particle size(s)) and ϑ_i^c is a phase shift. Importantly, in this regime κ_R becomes longer than the DH prediction (at $\kappa_D a \approx 2$), a phenomenon known as underscreening — where the screening length is longer than the DH prediction.

The result of Kjellander and co-workers result is not unique, and there have been multiple other notable theoretical approaches [141], and these have been discussed recently by Jäger et al. [142] and Espinosa-Marzal et al. [143]. Similarly, Carvalho and Evans [144,145] and Attard [146] derived theories based on analysis of the Ornstein–Zernike equation [147]; Bazant, Storey and Kornyshev (BSK) [148] used a Landau–Ginzburg treatment; Frusawa [149] and Gavish, Elad and Yochelis [122] used a modified Poisson–Nernst–Planck model, with

the latter work indicating that the onset of oscillatory behaviour is due to both the concentration and the asymmetry in the ion sizes. Ludwig et al. [150] derived an Ising model and Adar et al. [151] used a modified Coulomb kernel incorporating finite sized particles. Rotenberg et al. [152] derived the Landau fluctuation theory for bulk solutions. Additionally, there has been some interest in understanding the effect of a thermal gradient on the screening length [153].

The solution of statistical mechanical theories, such as the Bogoliubov–Born–Green–Kirkwood–Yvon hierarchy [154–157] or the Ornstein–Zernike equation [147], requires appropriate closure [158–160]. For the latter, several well-known closures have been used, such as the hypernetted chain equation, the Percus–Yevick equation and the mean spherical approximation (MSA). Each carries its own assumptions and approximations, and we point the interested reader to Refs. [159,160] for a complete discussion and derivation of the relevant results. Simplistic models of atoms are typically invoked in order to achieve an analytical solution, or even to simplify associated numerical calculations. For example, a common treatment of ions is the primitive model, which considers ions as oppositely charged hard spheres. Adding the additional constraint that all ions have equal size results in the restricted primitive model (RPM), which additionally employs a dielectric solvent medium. Owing to this ansatz the RPM can introduce unphysical artefacts that result in the decoupling of density–density and charge–charge correlations [58,161]. The use of a constant Bjerrum length (which corresponds to unscreened electrostatic interactions, see Section 2) and concentration-independent relative permittivity [43,162,163] is also problematic in this respect.

3.2. Simulating underscreening

Examining electrolyte underscreening via computational simulations is a natural extension to the first-principles treatments discussed in the preceding section, and an increasingly-utilised approach. There are two main approaches that are taken: classical density functional theory (cDFT) and molecular dynamics (MD). What is generally found is that in bulk there is an onset of oscillatory behaviour (Kirkwood point) at a certain concentration, and the prediction of screening in the normal regime (see Fig. 2). The screening length is typically extracted from the predicted densities via a calculation of the total charge correlation function [103,164]:

$$\psi_i(r) \sim g_{zz}(r) = g_{++}(r) + g_{--}(r) + g_{+-}(r) \quad (12)$$

where $g_{++}(r)$, $g_{--}(r)$, $g_{+-}(r)$ are the radial distribution functions of cations–cations, anions–anions and cations–anions respectively. This form can be simplified if a model such as the RPM is used that uses same-size, oppositely charged particles.

3.2.1. Classical density functional theory

cDFT models treat all ions on the same basis and with finite size, and are therefore able to recover the Kirkwood crossover point, and predict the existence of underscreening at high concentrations [142,165–167]. Generally cDFT studies also find agreement with atomistic MD simulations [142,165,168] (see below), but none have shown the presence of anomalous underscreening. However, cDFT does show oscillatory behaviour adjacent to a surface [167–170], consistent with SFB and AFM experiments at small separation distance (see Sections 4.1 and 5.1). Further discussion of cDFT results can be found in the recent paper by Jäger et al. [142]

3.2.2. Molecular dynamics

Many approaches to understanding underscreening (and electrolytes in general) make use of molecular dynamics (MD). These range in sophistication from the RPM in a dielectric continuum, to all-atom MD (with explicit solvent) which includes a more realistic treatment of intra- and intermolecular forces. Coles et al. [103] observed underscreening in bulk Na(aq), LiCl(aq) and LiTFSI in both aqueous

non-aqueous solvents. Their predicted screening lengths are shown in Fig. 5(a) and are in agreement with MSA calculations using the RPM [152]. Similarly, Zeman et al. examined underscreening in aqueous NaCl and $[C_4C_1im][NTf_2]$ in propylene carbonate in both bulk [104] and under confinement with graphene [171]. The very significant size and timescale of these simulations is noteworthy, as is the use of multiple oscillatory functions of the same form as Eq. (11) to determine the electrostatic decay length. An extension of the theory presented in Section 3.1 allows for the existence of multiple decay modes that can be either purely Yukawa (exponential), or oscillatory [58,172]. In the long-range limit, the mode that dominates, and hence measured, is that with the longest decay length. The results of Zeman et al. are depicted in Fig. 5(b), showing the decay lengths obtained from the multiple fitting.

Earlier work by Keblinski et al. [173] probed the phase space of molten and gaseous NaCl and showed the onset of the oscillatory behaviour, with two distinct decay modes clearly coexisting close to this point. This consisted of a short-range oscillatory mode, and a long range monotonic mode, reminiscent of the experiments described in the following section. Notably however, this result was achieved without an interface. The influence of confinement on the screening length in NaCl(aq) was considered by Finney et al. [174], who observed an increase in the screening length at higher concentrations, in line with surface force balance (SFB) results (see below). However, deviations from the DH theory were also observed in the concentration region where there is agreement between theory and experiment. Other investigations using constant chemical potential methods [142] do not find the scaling found by Finney et al., hence these results are deserving of further investigation.

Despite the complexity of the above simulations, the use of coarse grained simulations [104] and even more simplistic models (such as the primitive model with coarse grained solvent [175,176] or dielectric solvent [165,166,177]) capture much of the physics associated with the screening length [142,166]. The agreement seen between simulations of different complexities is most likely due to the Coulomb force dominating the behaviour. Notably however the multiple decay lengths seen by Zeman et al. are not recovered by these more simplistic treatments. Caution should be used to ensure that any MD simulation considers a region of the phase space probed experimentally, as pointed out by Härtel et al. [78].

4. “Anomalous” underscreening

Whilst the theory predicting underscreening (and other non-DH behaviour, such as the Kirkwood point) has been around for a number of decades, several experiments in the last 10 years have revealed underscreening contrary to predictions from theory and simulations discussed above (Fig. 2). Such underscreening is known as “anomalous” underscreening, to be differentiated from the “normal” underscreening that is predicted by theory [78]. It is thought to be of electrostatic origin [178] and was originally highlighted by SFB measurements of aprotic ILs by Gebbie et al. [83,179], who attributed anomalously large screening lengths to ion-clustering within the IL. It was hypothesised that the number of ‘free ions’ in the bulk is much lower than expected, and so the screening length is consequently larger. This hypothesis was made in the context of the then-ongoing debate regarding the ionicity of ILs [180–182]. However, mounting evidence in aqueous and non-aqueous electrolytes indicates that it is a general phenomenon not limited to ILs, and so is unlikely due to strong ion clustering. Moreover, to our knowledge scattering experiments have failed to detect the existence of long-lived clustering in ILs and concentrated electrolytes.

The hallmark of anomalous underscreening is the scaling exponent $\xi = 3$ in the following equation proposed by Lee et al. [89]:

$$\left(\frac{\lambda_S}{\lambda_D}\right) \sim \left(\frac{a}{\lambda_D}\right)^\xi \quad (13)$$

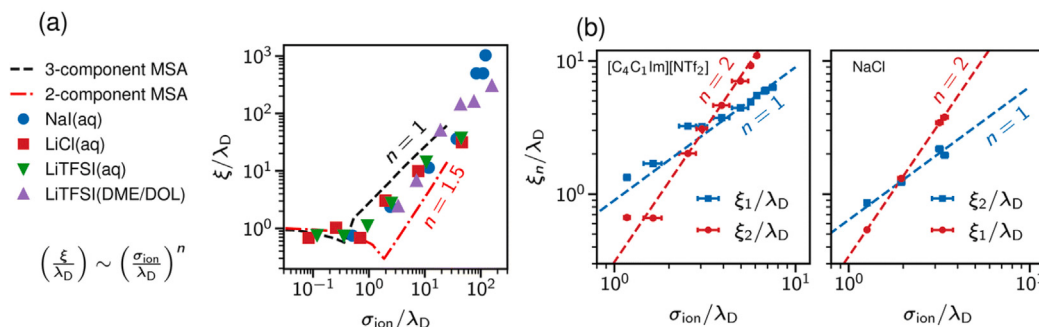


Fig. 5. Bulk MD simulation results using classical force fields, showing the scaling of the screening length (here denoted as ξ , rather than λ). The x-axis is in units of $\sigma_{\text{ion}}/\lambda_D$, where σ_{ion} is the ion size. (a) Coles et al. [103] (and the MSA results of Rotenberg et al. [152]). (b) Zeman et al. [104].
Source: Figure used with permission from Ref. [142].

where λ_S is the measured screening length and ξ an empirically-determined constant. Eq. (13) describes underscreening when $a/\lambda_D > 1$ (note $a/\lambda_D \propto \sqrt{I}$). DH behaviour corresponds to $\xi = 0$ in this equation, i.e. $\lambda_S = \lambda_D$, while underscreening corresponds to $\xi > 0$. Generally theory and simulations detailed in the preceding discussion find $1 \leq \xi \leq 2$, whereas anomalous underscreening finds $\xi \approx 3$ [78,89,178]. Despite some promising theoretical treatments aimed at elucidating anomalous underscreening, no simulation or theory has yet been able to explain this phenomenon consistently with experiment. The fact that experimental observations of anomalous underscreening are based on exclusively interfacial techniques (the majority of which are SFB measurements) suggests that anomalous underscreening itself could be an artefact of such techniques. Indeed, one recent article has suggested that the SFB only resonates with particular modes of the correlation function [183]; there is still a strong possibility that the presence of an interface itself may be required for anomalous underscreening to manifest. Nevertheless, simulated interfaces fail to produce anomalous underscreening according to the power law of Eq. (13) [171] (we return to a discussion of surface chemistry and confinement in Section 5). Therefore, to date, no satisfactory explanation for the existence of anomalous underscreening has been established in the literature. The discussion below therefore reviews the current state of experimental and theoretical investigations aimed at understanding anomalous underscreening.

4.1. Surface force balance measurements

The surface force balance is an experimental technique to measure the forces in a liquid by imposing compression or rarefaction between two crossed cylinders. There exist several variants of the technique, and some of these are known as a surface force apparatus (SFA). While there are subtleties in the implementations, herein we refer to all these as SFB, as was done in the recent review by Lin and Klein [185]. We also draw the readers attention to a very recent, and comprehensive, introduction and review of the SFA/SFB technique [186].

Just over a decade ago, SFB experiments were performed by Gebbie et al. on the IL $[\text{C}_4\text{C}_1\text{im}][\text{NTf}_2]$ confined between mica and gold [83], where the concentration of ionic species (ignoring any ion pairing/clustering) is 3.43 mol/L at 298.15 K. This gives a predicted Debye length (λ_D) of 0.06 nm. However, in fitting the decay of the force profile, they determined a screening length ≥ 10 nm at all the applied potentials tested. A subsequent work probing the effect of temperature repeated these experiments using the ILs $[\text{C}_2\text{C}_1\text{im}][\text{NTf}_2]$ and $[\text{C}_3\text{C}_1\text{im}][\text{NTf}_2]$. These experiments revealed that the screening decreased with increasing temperature, in contrast to that predicted by Eq. (5) [179]. While the relative permittivity does vary with temperature [43,187–189], the amount of variation of the permittivity for similar ILs [189] is less than the temperature variation, so with increasing temperature $\epsilon_r \cdot T$ still increases, and so λ_D is still predicted

to increase. The authors suggested the possibility that IL ion pairs have a significant energy barrier for dissociation, meaning that only the ions that underwent thermal excitation to the free states would contribute to screening. The concentration of these free ions must be significantly reduced compared to the total number of ionic species, i.e. $<0.1\%$ [83]. A review of several of the initial experiments also pointed out that if anomalous underscreening was due to entropic changes, this would be purely repulsive and would increase with temperature [178,190].

Independent SFB measurements by Smith et al. [79] extended the results of Gebbie et al. from ILs to electrolytes in general. Smith et al. examined aqueous NaCl, neat $[\text{C}_4\text{C}_1\text{pyrr}][\text{NTf}_2]$, $[\text{C}_4\text{C}_1\text{pyrr}][\text{NTf}_2]$ in propylene carbonate and some additional neat ILs, and showed a minimum electrostatic decay length (MEDL) at ≈ 1 mol/L for both the diluted IL and $\text{NaCl}_{(\text{aq})}$. At concentrations lower than this threshold, the decay length decreased in agreement with DH predictions, whereas above it the screening length increased. Lee et al. [88,89] subsequently showed that ion-specificity in this phenomena could be removed by considering normalised ion sizes and a relative permittivity fitted from experiment (see Fig. 6(a)), meaning that the observed anomalous screening lengths were consistently characterised by an exponent in Eq. (13) of $\xi = 3$ when $a/\lambda_D > 1$. Unfortunately, because data for large a/λ_D is difficult to obtain (particularly due to solubility limits), these experiments probed underscreening primarily within a single decade of ionic strength, as noted recently by Härtel et al. [78].

Multiple other SFB experiments have since been reported using mica interfaces with electrolytes ranging from water-in-salt solutions (water in LiTFSI [96], DES [94], IL systems [82,84,86,191–193] and aqueous solutions [81,95]. Such experiments consistently indicate the presence of anomalous $\xi \approx 3$ underscreening. A selection of these results is shown in Fig. 6(a). We note that at high a/λ_D , a deviation from this trend is seen, and while this could be due to the difficulty in estimating the diameter of the complex-shaped ILs [89], it is possible it also shows a break from the trend, so further investigation of this phenomenon at high a/λ_D values, especially if it can be done with spherical or symmetric ions, would be a useful endeavour.

SFB force curves generally reveal short-range ordering at the solid-liquid surface for small surface separations (indicated by oscillatory forces), followed by a long monotonic decreasing ‘tail’. When plotted on a log-linear curve, the gradient of the tail can be used to derive the screening length. Typically, changes in concentration, humidity, temperature or composition only affect the short range behaviour in such force curves [86,192,193]. Lhermerout et al. [191] undertook experiments at different approach rates of the SFB surfaces, and determined that hydrodynamic forces were not the cause of the anomalous screening lengths, despite examples of very slow equilibration dynamics, even up to or greater than 20 h [84,87,192]. Additionally, the presence of water, while showing a marked effect on some properties of ILs [33,194], appears to only have a minor effect on the decay length, and appears generally to cause a decrease of λ in ILs [84,192,195]

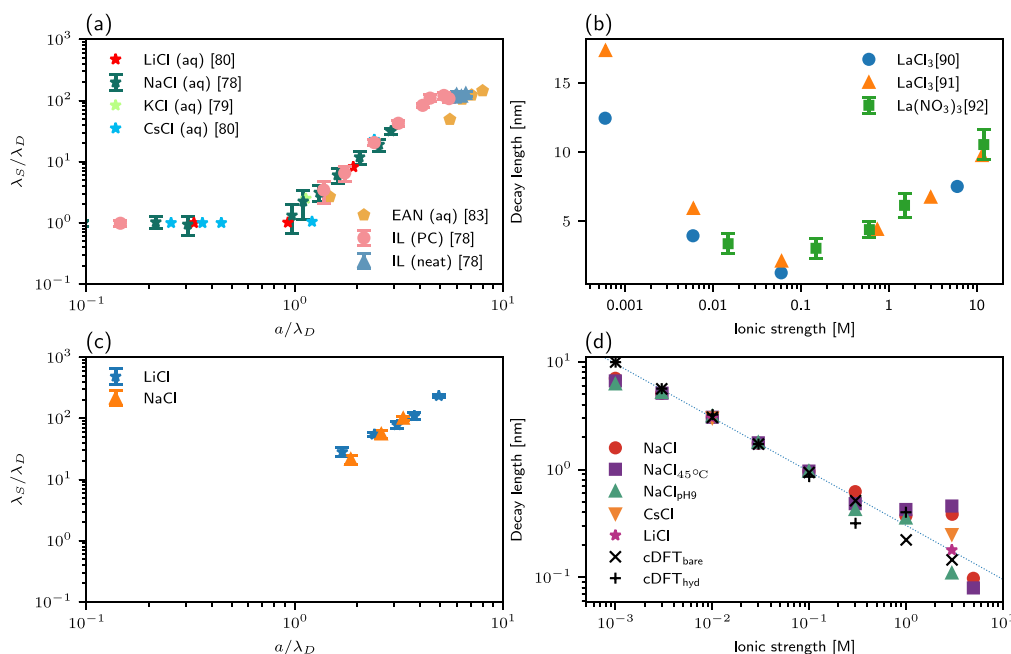


Fig. 6. Experimentally-observed anomalous underscreening. (a) Shows a selection of SFB experimental results for 1:1 electrolytes plotted as λ_S/λ_D vs. a/λ_D , showing the $\xi = 3$ scaling for $a/\lambda_D > 1$. (b) Decay lengths extracted from SFB experiments by Han et al. [93], and by Han et al. from other works [91,92], and plotted against ionic strength, showing the increase in screening length occurring after a minimum electrostatic decay length (MEDL) at ≈ 0.06 M ionic strength. (c) Fluorescence measurements from Gaddam and Ducker [101] with the same x -axis as in (a). (d) AFM measurements of various aqueous solutions by Kumar et al. [99]. Source: Data extracted using the tool by Rohatgi [184] and reproduced from Refs. [91–93,99,101].

and DES [94]. Similarly, while applied external potentials perturb electrostatic screening, they do not remove the observation of anomalous underscreening, for both mica-IL-gold [83] and mica-IL-mercury interfaces [82,196]. This suggests perhaps that the electric field from the surface need not be particularly strong across the apparatus for the anomalous underscreening to manifest. While the applied potential and surface chemistry (see Section 5.3) can cause variations in the screening, the choice of spring stiffness can also have a marked impact on the ability to resolve the long range forces [185,197].

Despite the predominant use of interfacial force measurements in this field, there have been suggestions that anomalous underscreening is a bulk phenomenon. Considering the SFB measurements of Smith et al. [79], which employed a neat IL (concentration ≈ 3.3 M), a screening length of 8.4 nm was reported. Taking one screening length from both confining surfaces gives a separation of 16.8 nm, covering almost the entire force-distance profile reported in that study. In this case the measurement therefore cannot be considered a *bulk* measurement. In contrast, the 2 M NaCl solution exhibited a screening length of only 1.1 nm, which corresponds to an overlap separation of 2.2 nm. Hence the majority of force-distance profile is outside at least one decay length. While the potential of the diffuse layer will not have completely decayed across only one decay length (see Section 2), the measurement will be less perturbed by the surfaces at greater separations, allowing for the possibility that true bulk behaviour is being measured. The respective contributions of the bulk and solid/liquid interfaces to anomalous underscreening therefore remain to be elucidated completely. Additional evidence was also provided by Lee et al. [89], showing agreement between calculations of the excess chemical potential (μ_{ex}) compared to that of bulk measurements (derived from the activity coefficients via $\mu_{\text{ex}} = k_B T \ln(\gamma)$), although Zeman et al. [171] have also pointed out that the underlying assumptions of the model used by Lee et al. [89] appears to break down for $a/\lambda_D \gtrsim 2.5$.

Finally, while most of the recent SFB results have been for 1:1 electrolytes, a recent publication by Han et al. [93] has shown a MEDL at ≈ 0.06 M ionic strength for the trivalent $\text{La}(\text{NO}_3)_3(\text{aq})$ (i.e. a

1:3 electrolyte) confined between mica surfaces. This study also re-evaluated prior results of $\text{LaCl}_3(\text{aq})$, also confined by mica, reported by Pashley et al. [91] and Tan et al. [92] (see Fig. 6(b)). These experiments show a clear deviation from DH-predicted screening at lower ionic strength in Fig. 2, and appear to follow the $\xi = 3$ anomalous scaling. Several other SFB experiments also report screening lengths similar in magnitude to these La^{3+} electrolytes. For instance, Adibnia et al. [90] considered $[\text{C}_6\text{C}_1\text{im}][\text{NTf}_2]$ in propylene carbonate confined between mica surfaces, while Hallett et al. [95] considered trimethylglycine (TMG) and KCl solutions, also confined by mica surfaces. Screening lengths in the latter study were attributed to a substantial increase in the relative permittivity of the liquid.

4.2. Fluorescence emission spectroscopy

A complementary technique that images an aqueous solution containing fluorescein molecules confined between borosilicate glass and an oxidised silicon wafer [198] has been used by Gaddam and Ducker [101] to study $\text{LiCl}(\text{aq})$ and $\text{NaCl}(\text{aq})$. The presence of the fluorescein molecule is directly detected by fluorescence emission, enabling the surface excess as a function of surface separation to be determined. By assuming the effect on the double layer of the fluorescein (a large divalent ion present at micromolar concentrations) is only a small perturbation, these experiments yielded screening lengths consistent with those observed by SFB, see Fig. 6(c). Anomalous underscreening is therefore not merely a manifestation of the SFB technique, or the presence of a mica substrate, for that matter.

4.3. Simulations and theoretical approaches

As discussed above, cDFT and atomistic MD approaches generally yield normal $\xi \approx 1 - 2$ underscreening behaviour. Whether or not anomalous underscreening, consistent with experimental observations, can be derived from current theories remains unclear. For instance, the mesoscopic theory of Ciach and Patsahan [199,200] finds some

agreement with the $\xi = 3$ scaling found by experiment, however it has been pointed out [142,151,171] that this is only achieved for $a/\lambda_d > 2.5$, whereas experiments exhibit anomalous underscreening for $a/\lambda_d \approx 1$ (for a 1:1 electrolyte). This theory also predicts that for $a/\lambda_d > 4$ the value of ξ should increase further, however there does not appear to be any evidence of this trend from experiments. For instance, screening lengths in SFB experiments appear to plateau at high concentrations (see Fig. 6(a)), although we note that the determination of the value of a for IL ions (which dominate this data) is questionable, as this value implicitly assumes that ions are spherical. Similarly, a recent paper by Härtel et al. [78] using molecular dynamics (MD) simulations of ions under the restricted primitive model (RPM) has also suggested good agreement with experiment, but requires the assumption of significant ion pairing (see Section 5.5). However, these MD simulations are in agreement with the Ciach and Patsahan theory, in that at higher a/λ_D , ξ increases. This was also observed by Zeman et al. [171] using the inverted model of Lee et al. [89] and experimental activity coefficient data.

5. The “known-unknowns” of anomalous underscreening

Based on the growing body of evidence discussed above, there are a number of “known-knowns” associated with anomalous underscreening. For instance, anomalous underscreening appears to be a general phenomenon for monovalent electrolytes in aqueous and non-aqueous solvents. It is also observed in molten salts, such as ILs. Nevertheless, there are still many “known-unknowns” regarding anomalous underscreening — factors that are potentially relevant to understanding the origins of anomalous underscreening that are yet to be considered, or resolved completely. The aim of the discussion presented below is to draw attention to these factors, in an effort to highlight possible avenues for future research.

5.1. Interfacial geometry

Interfaces fundamentally influence physicochemical phenomena. Notably, the chemistry and electronic structure of solid surface(s) influences both structural and temporal properties of electrolyte interfaces [178]. For example, it has been shown that reversals in the Hofmeister series for the observation of yield stresses are dependent on the chemical structure of the surface (mica versus alumina) [201,202], with theory suggesting this arises from hydration and nonelectrostatic (i.e. dispersion) effects [203]. Similarly, Schwierz et al. have shown that the ordering of the Hofmeister series depends on the surface charge and the polarity (hydrophobic versus hydrophilic) [204].

As noted above, there is ongoing debate regarding whether or not underscreening is a bulk or interfacial phenomenon. The vast majority of experimental evidence of anomalous underscreening is, however, obtained from interfacial measurements. In this respect, the geometry of the interface itself is also likely a key factor, and the study of electrolytes under confinement has been discussed very recently by several groups [205–207]. Simulations by Zeman et al. [171], which considered electrolyte solutions confined between graphene monolayers, did not yield anomalous underscreening. In contrast, a recent approach by Gurina et al. [208] did indicate some agreement.

The issue of interfacial geometry is succinctly illustrated by comparing SFB results with those obtained using AFM. The former almost exclusively yields anomalous underscreening ($\xi \approx 3$, Eq. (13)), while the latter generally yields normal underscreening ($\xi \approx 1.5–2$, Eq. (13)), as shown in Fig. 2. AFM has been widely used to study ionic solutions and the structure of the solid–liquid interface; it can also be used to measure force-distance information, analogous to the SFB. However, while the SFB typically uses surfaces interacting across the liquid of interest with a radius of ~ 1 cm, AFM generally utilises a flat surface (upon which the solution of interest is placed) and either a colloid probe (with radius of 1–15 μm) or a bare tip (with radius of curvature,

R , of 1–100 nm) interacting across the liquid of interest. Hence there is a higher degree of geometric confinement in the SFB than in the AFM. Smith et al. [100] employed a colloid probe to examine screening in a series of symmetric (i.e. n:n) electrolytes (NaCl, CsCl, CuSO_4 , MgSO_4 , LaFe(CN)_6) on a silica particle substrate. Results obtained deviated from DH theory for the di- and trivalent salts at low concentrations, while the monovalent salts were in agreement with DH theory over the concentration range studied (0.01–100 mM); a result attributed to the presence of ion pairs. A similar conclusion was reached by Stojimirović et al. [209] for LiCl and tetrabutylammonium chloride (TBAB) in isopropanol. Since the concentration range of these two studies was still < 1 M, whether underscreening here is normal or anomalous is unclear. Kumar et al. [99] investigated several aqueous alkali halide solutions (using an AFM tip with $R = 252$ nm) and also failed to observe $\xi = 3$ anomalous underscreening. Instead their measurements were in agreement with cDFT results [165], see Fig. 6(d), and were not sensitive to the identity of the substrate (silica vs. mica). We note here also that only a moderate deviation is seen from the DH prediction itself in these experiments. Silica colloid probe measurements by Hjälmarsson et al. [210] of the IL ethylammonium nitrate (EAN) on a mica surface suggested that anomalous underscreening could be switched on at temperatures above 373 K. This result is contrary to the smooth temperature dependence observed by Gebbie et al. [179] using SFB, and also recent SFB measurements of EAN confined by mica by Fung and Perkin [84] which demonstrated that the long range decay manifests at all temperatures. Potentially, the manner in which temperature is controlled is therefore an important factor [211].

5.2. Surface-adsorbed ions

While the geometry of the interface is a likely factor associated with the manifestation of anomalous underscreening, the dynamics of the electric double layer (EDL) appear less influential. For aqueous solutions with simple inorganic ions, simulations using Brownian dynamics have suggested that the relaxation of the double layer following electron transfer ranged from 0.40 ns at 0.11 M to 0.05 ns at 1.02 M. Additionally, this value decreased when the surface charge density was higher [212]. In contrast, ILs, due to the inherent asymmetry of their constituent ions and higher viscosities, undergo structural relaxations on far longer timescales. For example, Han et al. [87] performed X-ray scattering and SFB measurements on both dry and wet imidazolium-based ILs, and saw layers near the surface form over a timescale of ~ 24 h. Belotti et al. [213] showed that an electric field persists near the interface (after an initial voltage pulse) for up to 100 h (depending on the IL). The screening length determined by Han et al. was characteristic of anomalous underscreening. Nevertheless, mean field EDL theories are unable to describe correlation effects at high electrostatic strengths, which can be determined by the following parameter due to Netz and coworkers [116,214]:

$$\Xi = \frac{2\pi\sigma\lambda_B^2q^3}{e} \quad (14)$$

where σ is the surface charge density, q is the ion valence and e the electron charge. For $\Xi \gtrsim 10$, the correlation effects between the liquid and the surface will be substantial enough to deviate appreciably from the mean field models described earlier [116] (Section 2).

While the Stern layer is generally thought to be a single layer of counter ions, there have been various theoretical treatments that have suggested alternating charge layers adjacent to the surface, causing an oscillatory charge profile (known as overscreening) normal to the interface [74,148]. This is thought to influence the screening length, and recent X-ray reflectivity measurements [215,216] of high concentration aqueous RbCl and RbI on mica suggested that the thickness could extend to ≈ 2 nm. The exact effect of this surface layering on the nature underscreening has been examined in SFB experiments by Gebbie et al. [83]. In a similar vein, Fung [82] varied the applied

potential across the interface — which would invariably change the structure of the Stern layer (or adjacent overscreening layers) — yet anomalous underscreening was still observed (although the magnitude of the screening length changed). Recent measurements by Belotti et al. [213] using electrochemical methods suggested the presence of overscreening and crowding behaviour, and quartz crystal microbalance (QCM) experiments using aqueous solutions of $[C_4C_{1im}]Cl$ and $NaCl$ suggested that above ≈ 1 mol/L, the structure at the surface becomes independent of the concentration [217].

Decoupling the pure geometric effects from the chemical/electrical nature of the interface is extremely challenging experimentally, and this represents a unique opportunity for theoretical and simulation approaches to provide further insight on this point.

5.3. Surface chemistry

The experiments discussed in (Section 4.1) have employed a range of surface materials, e.g. gold, mica, silica and mercury. Of these, mica and silica are the most commonly employed in SFB (and AFM) experiments. However we note that other materials in SFB apparatus, i.e. gold and mercury, also produce anomalous underscreening, and this is irrespective of whether the SFB experiments use symmetric or asymmetric substrate configurations. Nevertheless, disagreement between experiments has led to suggestions that the probe surface influences underscreening itself. In particular, the AFM experiments of Kumar et al. [99] did not show anomalous underscreening using aqueous solutions confined between a silica tip and silica substrate. Switching the silica substrate for mica led to the same conclusion. Similarly, AFM measurements of EAN confined by a silica colloid probe and mica [210] and SFB [84] using mica, yielded contrasting results across a wider range of temperatures. However, the degree to which these differences arise from the silica/mica surface chemistry is yet to be resolved. It is conceivable that they are pertinent; for instance, while mica is cleaved to yield an atomically smooth surface, silica has non-zero surface roughness. While the arrangement of Si^{4+} and the Al^{3+} at the mica surface and subsurface gives rise to structural heterogeneity, inferred from the short-range ordering recently found with an AFM [218], the silica surface is more chemically uniform. Both materials have surface OH groups [218–220] and it has been shown for silica that there is constant protonation and de-protonation of these OH groups. This causes temporal heterogeneity that has been observed on the micrometre scale [116,221]. It is possible that this also occurs on mica, however this is yet to be confirmed. Both materials have low isoelectric points [222] (silica < 3 , mica < 3.5) with experiments typically done above these values, where the surface contains a net negative charge.

5.4. Interfacial confinement

The effects of confinement, especially with respect to the transport of ions, is well established, and has been the subject of several reviews [205–207]. The restriction imposed by the interfacial geometry has also been shown to affect various properties of liquids, as discussed recently [205,206,223]. In particular, the relative permittivity (i.e. the dielectric constant) becomes tensor-valued ($\epsilon_{\perp} \neq \epsilon_{\parallel}$), and exhibits different real and complex electrodynamic responses [224]. Both $\epsilon_{\perp}$ and $\epsilon_{\parallel}$ change, and in particular the value of $\epsilon_{\perp}$ is reduced overall and exhibits a spatially varying profile away from the surface [206]. Since the forces are measured normal to the surface in both SFB and AFM, we focus on the perpendicular component $\epsilon_{\perp}$ in our discussion here.

Confinement causes $\epsilon_{\perp}$ to decrease when the separation between the surfaces is < 100 nm, as shown in Fig. 7 for both pure water [225–229] and aqueous solutions [230–232]. This result was attributed to a restriction of dipole motion [225], however it has also been suggested that this is caused by the electronic structure of the solid [227]. While the experiments by Fumagalli et al. employed hexagonal boron nitride

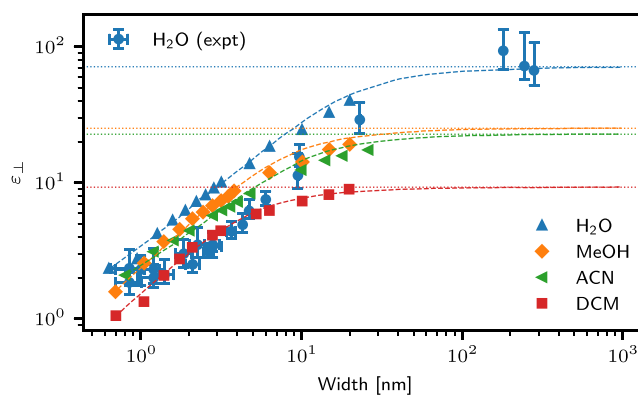


Fig. 7. The perpendicular dielectric permittivity estimated from simulations of several solvents in a graphene slit by Motevaselian et al. [235] and experimental measurements by Fumagalli et al. [225] of water in h-BN/graphite, showing the decrease of the perpendicular relative permittivity due to confinement, which occurs from a significant distance from the surface.

Source: Data reproduced from Refs. [225,235].

(h-BN) and graphite surfaces (both hydrophobic), simulations have indicated that it occurs on other substrates [233], including hydrophilic surfaces [234]. It was also shown to occur with other solvents by Motevaselian et al. [235] (Fig. 7). Several theories have been successful in modelling this phenomenon [236,237]. Critically however, the range at which $\epsilon_{\perp}$ begins to reduce in Fig. 7 coincides with the distances relevant to the measurement of electrostatic screening lengths using SFB, AFM and fluorescence techniques described in Section 4.1, and this extra contribution is not taken into account in calculations of λ_D in these studies (although the concentration dependence of ϵ is accounted for).

The influence of confinement has also been considered from a theoretical standpoint. Recent simulations by Zeman et al. [171] using graphene to confine the electrolyte did not show any stronger scaling than $\xi = 2$, consistent with their earlier work [104]. In an attempt to obtain a better description of the structure around the surface, these authors subsequently used a variety of methods including grand canonical MD [142] and cDFT [142,166], however both methods predicted similar screening lengths from the Kirkwood point ($a/\lambda_D \approx 1$) to around $a/\lambda_D \approx 3$, at which the point the effects of hard-core repulsion become the leading term and became sensitive to solvent choice and ion size. Building on their previous work, Ciach and Patsahan [238] applied their theory to a model slit geometry. They were able to show oscillatory density profiles normal to the interface, and similar to their theory in the bulk, they find some agreement with the $\xi = 3$ scaling, however this is at larger values of a/λ_d than employed experimentally. Ciach and Patsahan's theory is also unable to reconcile the absence of anomalous underscreening seen by Kumar et al. [99] using AFM. It has been suggested by Huang [239], using BSK theory [148], that confinement causes ion-pair dissociation to become unfavourable. Thus, the number of free ions would be vastly reduced and the screening length would therefore increase. Other reports suggest that confinement can cause the violation of charge-neutrality (i.e. where there is unmatched charge within some region) [240,241], and this would be more likely to occur in a SFB due to the confining geometry.

5.5. Ion pairing vs. Ion correlations

There have been many suggestions from various works that the origin of anomalous underscreening is due to ion pairing or clustering [78,83,167,177,239,242], which would decrease the effective concentration of ions (i.e. behave more like a dilute electrolyte). Ion pairing itself is still widely debated, and has been the subject of

numerous reviews [243–249]. The DIT theory discussed in Section 3 allows for a broader description of ion–ion correlations than is incorporated into either the dressed charge q_i^* or $\mathcal{E}^*(k)$ (Eqs. (7), (8)). We have also recently shown that for alkali metal chlorides, the ion pair interactions are incredibly dynamic and concentration dependent, and in many cases do not outlive the natural relaxation times of water [250]. This draws into question the importance of ion pairing on macroscopic phenomena such as underscreening. Additionally, there are several works that also suggest that ion pairing cannot be used to explain underscreening. For example, Feng et al. [69] performed non-polarizable MD, and examined how ion pairing and clustering influence dynamic properties of $[\text{C}_4\text{C}_1\text{im}][\text{TFSI}]$, and specifically how these were affected by pairing and clustering. These simulations suggested that, while there is a significant association between the cations and anions (corresponding to a free ion percentage of $\sim 15\%$), it is not sufficient to explain experimental results. It was similarly found that the degree of ion pairing is insufficient through an analysis of Bjerrum pairing by Adar et al. [251], and by Goodwin and Kornyshev [74] via analysis of the differential capacitance. Further, spectroscopic measurements in aqueous systems do not show an abrupt change about the Kirkwood point, and also do not evidence the amount of ion pairing required to reduce the free ion concentration to result in anomalous underscreening [252–254].

The use of ion–ion correlation, as opposed to ion–pairing, is a more encompassing paradigm, and allows for a rigorous inclusion of nonlocal electrostatics. It also allows for the contribution of any associated species which are still expected to contribute to screening as a dipole (rather than a neutral species). In fact, Kjellander has pointed out that the decay of a solution-phase dipole actually has the same decay behaviour as a lone ion (i.e. a Yukawa-like decay with the same decay length) [255]. The inclusion of zwitterions to a solution is a good test for this, and was shown to markedly increase the screening length [95]. Additionally, Zaurbin and Bier have suggested, based on simulations of a dipolar fluid, that the length scale of investigation can manifest different behaviour for the same system. It has also been pointed out recently [143] that measurements of conductivity, while deviating from Nernst–Einstein conductivity behaviour (due to correlations between the ions), cannot account for anomalous underscreening. Further, ILs do not show sufficient deviations from the behaviour of aqueous KCl solution (assumed fully dissociated) [180]; the authors here have stated that the influence of all the neighbours is more influential than a single pair, and that they appear to move predominantly in an uncorrelated manner. Finally, it has been suggested by several studies that the lifetime of ions is particularly important in describing macroscopic properties. For example, the lifetimes correlate better with the conductivity [256,257] (also found by spectroscopy measurements [73]) and the ionicity [25,26].

5.6. Quantum and many-body effects

Quantum chemical simulations of liquids are difficult, owing to the configurational complexity. However, we suggest (in a similar vein to Parsons et al. [258]) that the absence of quantum mechanical modelling of the liquid state will continue to be a detriment to our understanding of anomalous underscreening. While classical models, which generally use spherical particles, are able to replicate much of the structural information in an electrolyte (e.g. hyperuniformity [200,259,260]), it is plausible that the delocalisation of the electronic density around ions in electrolytes is related to the emergence of underscreening at high salt concentrations. For instance, KS-DFT calculations recently reported by Kathmann and co-workers [42,261] show significant electric fields in aqueous NaCl solutions, and were suspected to underpin crystalloluminescence — the emission of UV light upon crystallisation.

Suggestions of long-range correlations on the nanometre scale [262] and plasma-like collective behaviour [263–265] have also been hypothesised, with frequencies in the THz regime. It is possible geometrical

confinement may be required for this to manifest (akin to quantum dots). Apostol was able to derive the $\xi = 3$ scaling law by assuming the existence of dispersive plasmons [263] and suggested that the oscillators are quantum mechanical in nature. It is therefore conceivable that electrolytes at very high concentrations are able to become pseudo-crystalline, leading to infinitely large screening lengths due to long-range ordering [173].

Nuclear quantum effects (NQE) have also not been investigated in the context of anomalous underscreening, despite the marked changes in the properties of condensed phases associated with replacing H_2O with D_2O . In water and other hydrogen-bonding solvents, the smaller mass of ^1H makes it more susceptible to tunnelling meaning that it behaves in a more delocalised manner [266,267]. These effects are particularly significant at low temperature [268]. At room temperature the structural and mean-field properties (e.g. static permittivity) are usually similar [267,269,270], but dynamic and/or instantaneous properties show significant differences, as they are a result of random fluctuations [267].

NQE have been shown to be important in ion solvation [271,272], and the use of D_2O can lead to a significant difference in the solubility limits of various salts [273], as well as differences in the osmotic and activity coefficients [274]. While in bulk solution the effects of heavy water substitution are more pronounced for dynamical properties, recent nonlinear spectroscopic experiments by Dupertuis et al. [275] of 3D confined water determined that the confinement effect of H_2O exists over distances >100 nm. In contrast D_2O was much less affected by the restriction of geometry. SFB experiments by Shrestha et al. [269] have also shown differences in the adhesion energy in these two solvents. Very recently, theoretical work has suggested that a quantum treatment of confined water will induce subtle differences in the behaviour near the surface compared to a classical treatment, and these can propagate to result in non-negligible differences in the electrostatics in the bulk [276]. In light of these results we contend that exploring the effect of NQE on electrostatic screening length should be a priority for future research.

By contrast, a number of studies have elucidated the role of dispersion forces in electrolytes and molten salts. For instance, it is known that better descriptions of SFB experiments are achieved by the inclusion of dispersion interactions [278], and this was used by Pashley et al. to explain the “hydration” force [279]. In ILs, dispersion typically contributes 8%–15% [280–282] of the total IL interaction energy, and so its inclusion is clearly important [283]. However, given the magnitude of the dispersion interaction is less, and it decays faster than the Coulombic interaction (i.e. $1/r^6$ versus $1/r$, respectively), the long-range interactions are expected to be dominated by electrostatics. Given that anomalous underscreening did not manifest in either the all-atom MD by Coles et al. [103] or those of Zeman et al. [104,171], it is unlikely it is the cause of the $\xi = 3$ scaling (since dispersion is included approximately via the molecular dynamics force fields used). Nevertheless, Kjellander and Ramirez [133] have suggested that coupling exists between the electrostatic and dispersion interactions, and this affects the form of the long-range decay. The use of correlated wave function methods that recover the dispersion interactions (e.g. Møller–Plesset Perturbation Theory [284] etc.), or more sophisticated treatments of electron correlation (e.g. the random phase approximation (RPA) [285]) would enable this coupling to be examined directly. A recent FMO-MP2 [286] study of the IL $[\text{C}_2\text{C}_1\text{im}][\text{BF}_4]$ demonstrated that the use of such approaches for large-scale simulations of complex condensed phases are now within reach [287]. Similarly, DFT and machine-learning forcefields [288] may assist in this respect, although we note that appropriate care must be taken to select an appropriate level of theory, as many DFT functionals do not properly reproduce the properties of water [289].

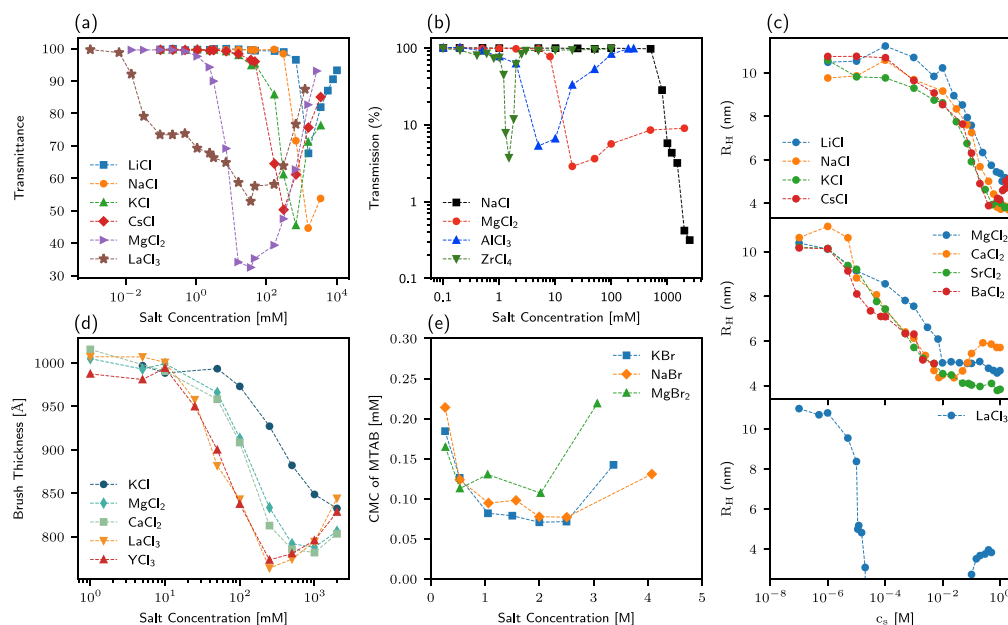


Fig. 8. Examples of reentrant behaviour observed in various soft matter systems. Transmittance of light through a solution containing silica nanoparticles, with various salt solutions by (a) Yuan et al. [61] and (b) Kumar et al. [62]. (c) Contractions and re-swelling of free polystyrene sulfonate with various monovalent (top) divalent (middle) and trivalent (bottom) salts. These data from Jia et al. [277] is plotted without error bars. (d) Reswelling of a polyelectrolyte PMETAC brush by Robertson et al. [102] (e) The effect of salt on the CMC of MTAB, from Yuan et al. [61].

Source: Data reproduced from Refs. [61,62,102,277].

5.7. Multivalent electrolytes

Despite the biological relevance of multivalent ions, there has been relatively few investigations of them in the context of underscreening phenomena. Multivalent electrolytes are generally more challenging than studies of monovalent electrolytes; ideally, measurements are made under conditions of high surface potential, however multivalent electrolytes greatly impact the surface potential under a wide variety of conditions, often adsorbing and leading to charge reversal, complicating investigations of the extent of the double layer. Multivalent electrolytes are also poorly described by the PB theory (see Fig. 3), and are characterised by much stronger ion-ion correlational effects. This has been suggested to result in charge inversion and so-called like-charge attraction between surfaces [290–292]. Nevertheless, the role of ion-clustering and strong Coulomb coupling in this context is yet to be established. A limited number of studies, nevertheless, have demonstrated the existence of underscreening in multivalent electrolytes. For instance the SFB measurements on 1:3 electrolytes discussed in Section 4.1 [91–93] showed a MEDL at a significantly reduced concentration (≈ 0.06 M) followed by anomalous underscreening. Smith et al. [100] showed deviations from DH theory, but restricted the scope of the study to low ionic strengths. Pashley and Israelachvili [279] performed experiments on alkaline earth metal chlorides and showed for 3 M MgCl_2 and 5 M CaCl_2 decay lengths of 1.8 nm and 2.0 nm respectively. Parsons et al. [278] suggested these results were due to dispersion, finding good agreement with theory. The absence of an anomalous screening length in these studies is most likely due to a reversal of the surface potential. More recent measurements by Perez-Martinez and Perkin using the dicationic IL $[\text{C}_{10}(\text{C}_1\text{im})_2][\text{NTf}_2]$ also did not show anomalous underscreening [293]. While Kohonen et al. [97] examined NaCl , MgSO_4 , $\text{K}_4\text{Fe}(\text{CN})_6$ and $\text{Th}(\text{NO}_3)_4$ solutions using SFB, concentrations were not sufficiently high to observe underscreening. There is therefore a clear need for surface force measurements of these systems at higher concentrations, particularly since there is a clear impact on so-called reentrant behaviour on polyelectrolyte swelling and other phenomena. We discuss such phenomena in greater detail below.

5.8. Electrochemical approaches

The differential capacitance (DC) of electrolytes has been discussed in the context of underscreening in several studies. The DC of an electrolyte relates the surface charge density to the potential. It has been predicted [148], simulated [169,294] and measured [295], to change due to overscreening and crowding effects at the electrode interface [158,296]. While much of this change is close to the surface, it is likely that these effects can propagate out into the bulk. These predictions and measurements of the DC challenge the massive ion pairing often invoked to explain anomalous underscreening [74]. For instance, Lee et al. [88] used a theoretically derived value of the DC for the IL $[\text{C}_2\text{C}_1\text{im}][\text{NTf}_2]$, which was compared to experimental measurements. They found agreement at low concentrations, however there was disagreement as the predicted capacitance (based on their large value of λ) was significantly lower than measured. It is conceivable that the screening length could also be extracted from alternative electrochemical measurements, such as impedance spectroscopy [297], as the Debye length enters such quantities as the Debye time (τ_D) [298]. Despite this opportunity, many, if not all, impedance spectroscopy experiments are performed at concentrations ≤ 1 M, likely due to the reasons outlined by Borodin et al. [17]. Such experiments will also be subject to the confinement and surface chemistry effects, as discussed above.

5.9. Underscreening and reentrant phenomena

The influence of increasing ionic strength on the stability of colloidal and macromolecular materials is well established. There have been several recent reports, however, of *reentrant* behaviour in these systems at high salt concentration, whereby colloidal or macromolecular materials redisperse/dissolve into solution. A selection of experimental reentrant work is shown in Fig. 8. In two examples of reentrant behaviour of silica nanoparticles (Fig. 8(a,b)) [61,62], nanoparticles are dispersed at low concentrations of salt (high transmittance of light), followed by flocculation (reduced transmittance), then increased transmittance again at higher salt concentration. It is noted this behaviour is not observed for some of the 1:1 electrolytes though. The

turn around point (or MEDL, assuming reentrance is driven by electrostatic interactions) in each of these cases is reduced when higher valence cations are used, in agreement with the SFB experiments of trivalent cations discussed in Section 4.1. Fig. 8(c) shows that the hydrodynamic radius of sodium polystyrene sulfonate (NaPSS) as a function of increasing concentration of various 1:n electrolytes is also an example of reentrant phenomena for several salts. This effect appears particularly enhanced for multivalent salts [277]. There are many additional examples of this phenomena in the literature; for instance, the solubility of DNA in the presence of tetravalent spermine [67], NaPSS in $\text{LaCl}_3(\text{aq})$ [299], chemically modified cellulose in various electrolytes [300], the force on micrometre sized particles in optical tweezers [301], coagulation of proteins [63,302] and in scattering of micellar solutions in deuterated water and deuterated DES [64]. Various other examples can be found where there is either an observed or predicted reversal of a behaviour with the origin likely to be electrostatic interactions [303–309]. Recent conductance measurements of ion-channel transport showed so-called biphasic behaviour [310], suggesting a possible common origin with reentrant phenomena. Further, another SFB work reported that a (neutral) poly(ethylene glycol) polymer brush extended further into $[\text{C}_2\text{C}_1\text{im}][\text{TFSI}]$, compared to water [311]. Correlations between colloidal nanocrystals dissolved in both molten salts or ILs was shown to extend well beyond the Debye length [312].

An analysis of existing polyelectrolyte literature by Liu et al. [313] suggested that the reentrant behaviour was due to the increase in the screening length that occurs at high salt concentrations, i.e. due to underscreening. Unfortunately, many of these experiments do not report or measure a value for λ , so it is unknown which, if any, of these reentrant systems exhibit anomalous underscreening. However, one notable simulation has suggested that normal underscreening resulted in reentrant behaviour of nanoparticles in monovalent salts [314]. Similarly, Robertson et al. [102] performed neutron scattering on a poly-(2-(methacryloyloxy)ethyl) trimethylammonium (PMETAC) polyelectrolyte polymer brush in the presence of 1:n electrolytes, see Fig. 8(d), and quantified the screening length (denoted λ_s^*). It was shown that it decreased initially, before increasing above ≈ 1 M ionic strength. Importantly, the underscreening observed was consistent with normal underscreening ($\xi \approx 2$). The critical micelle concentration (CMC) of the surfactant myristyltrimethylammonium bromide (MTAB) in aqueous electrolytes (Fig. 8(e)) also shows an initial decrease with salt concentration, followed by an increase above ≈ 2 M [61]. These results therefore highlight an as-yet underutilised route for elucidating the nature of underscreening. We believe that further study of soft matter and colloidal reentrant phenomena in highly concentration electrolytes (>1 M) should be an important area of focus in this field.

6. Summary and outlook

Despite enormous effort, there is still no universally accepted explanation of anomalous underscreening. The study of electrolytes and liquid structure is clearly far from complete, and continued exploration and discovery provides a unique opportunity for experiments, simulations and theoretical treatments to provide multifaceted insight into the origins of this intriguing phenomenon. Validation of recent theoretical treatments [78,138,172,199,238,276] can increasingly be achieved with an ever increasing computational capability [315,316] in conjunction with improved models of electronic structure and force-field sophistication (i.e. explicit polarisation [317,318] or inclusion of NQE [267,319,320]). Similarly, experimental techniques continue to deliver improved sensitivity and sophistication, as evidenced by X-ray photoelectron spectroscopy [321], and X-ray scattering [215, 216] approaches to imaging the electric double layer. Additionally, van Hove correlation functions [322], generated from inelastic X-ray or inelastic neutron scattering [48,49,323,324], or computed directly using atomistic MD [50,250,325], afford both spatial and temporal

information of electrolyte structure, including ion-solvent correlations. Optical techniques such as dielectric relaxation spectroscopy [326–328], 2DIR [329–331], and other ultrafast/nonlinear techniques [51, 54,72,73,246,328,332–342] also promise to improve understanding of liquid spatial and temporal behaviour, as do prospective techniques such as X-ray SFB [343], which enable concurrent measurement of force and structural information.

Given that many techniques involve an interface, there is an imperative to establish a truly bulk measure of the screening length (to decouple surface effects). Measurements by Shelton [341] using hyper-Rayleigh scattering have shown excellent agreement with DH theory at low concentration, and this holds promise for bulk measurements of highly concentrated (>1 M) electrolytes. There has also been a recent study that mapped the electrostatic potential around ions [344] in a 1 M electrolyte. This approach provides a further avenue of bulk solution investigation. The principal opportunity facing computational researchers in this field is the use of electronic structure calculations to understand underscreening, considering the molecular nature of solvents themselves and the fact that electron density is non-local. We hope that this perspective encourages future work to unravel the complex nature of electrolytes and the origins of anomalous underscreening.

CRediT authorship contribution statement

Gareth R. Elliott: Writing – review & editing, Writing – original draft. **Kasimir P. Gregory:** Writing – review & editing. **Hayden Robertson:** Writing – review & editing. **Vincent S.J. Craig:** Writing – review & editing. **Grant B. Webber:** Writing – review & editing. **Erica J. Wanless:** Writing – review & editing. **Alister J. Page:** Writing – review & editing, Conceptualization.

Declaration of competing interest

The authors declare the following financial interests/personal relationships which may be considered as potential competing interests: Alister Page reports financial support was provided by Australian Research Council. If there are other authors, they declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

Data availability

No data was used for the research described in the article.

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